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Algorithms and Complexity
Christian Schindelhauer

Mobility in Wireless Networks

Invited Talk for SOFSEM 2006

Měříň, Czech Republic

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**Heinz Nixdorf Institute
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➤ **Introduction**

- Wireless Networks in a Nutshell
 - Cellular Networks
 - Mobile Ad Hoc Networks
 - Sensor Networks
- Mobility Patterns
 - Pedestrian
 - Marine and Submarine
 - Earth bound Vehicles
 - Aerial
 - Medium Based
 - Outer Space
 - Robot Motion
 - Characterization of Mobility Patterns
 - Measuring Mobility Patterns

➤ Models of Mobility

- Cellular
- Random Trip
- Group
- Combined
- Non-Recurrent
- Particle based
- Worst Case

➤ Discussion

- Mobility is Helpful
- Mobility Models and Reality

Introduction

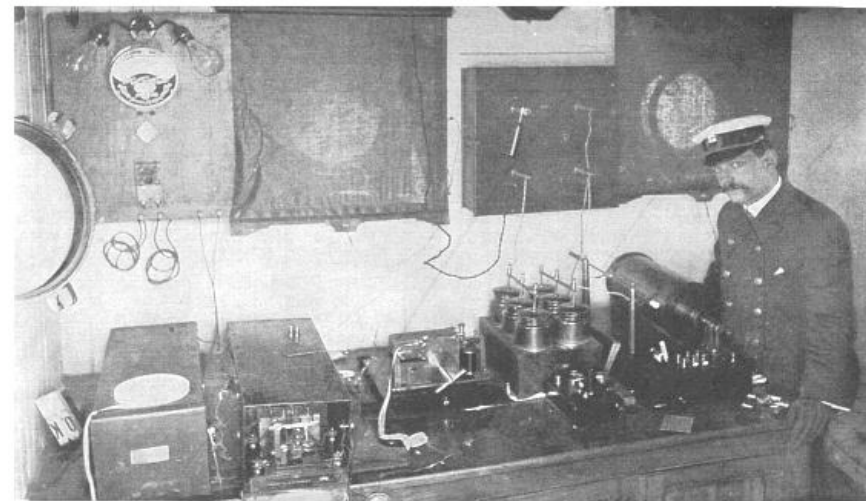
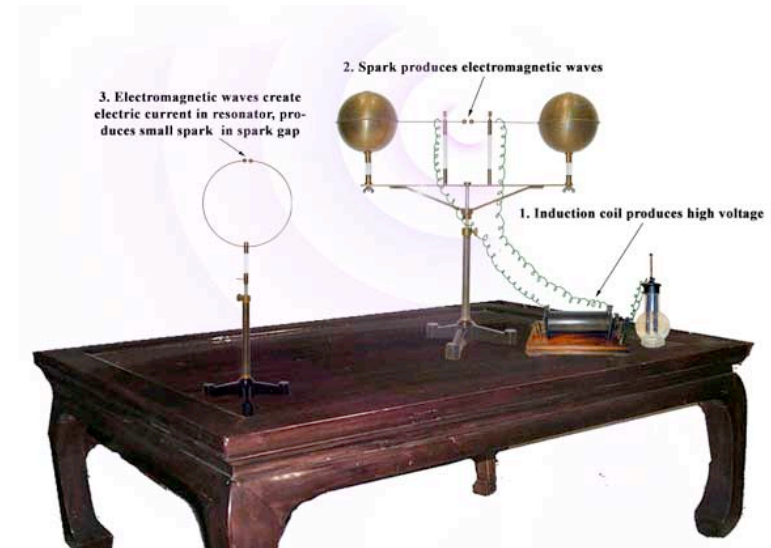
The history of Mobile Radio (I)



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- 1880s: Discovery of Radio Waves by Heinrich Hertz
- 1900s: First radio communication on ocean vessels
- 1910: Radios required on all ocean vessels



THE "MARCONI MAN" AND HIS INSTRUMENTS

Introduction

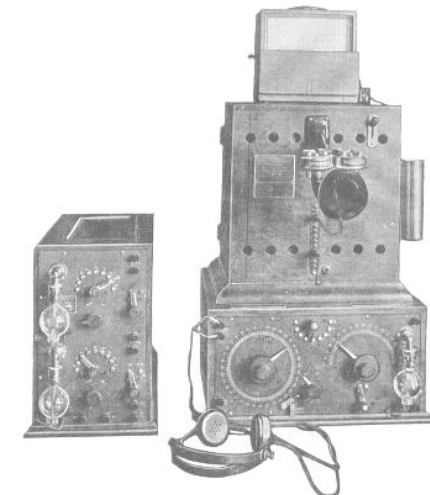
The history of Mobile Radio (II)



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- 1914: Radiotelephony for railroads
- 1918: Radio Transceiver even in war air plane
- 1930s: Radio transceivers for pedestrians: "Walkie-Talkie"
- 1940s: Handheld radio transceivers: "Handie-Talkie"



RADIOTELEPHONY APPARATUS

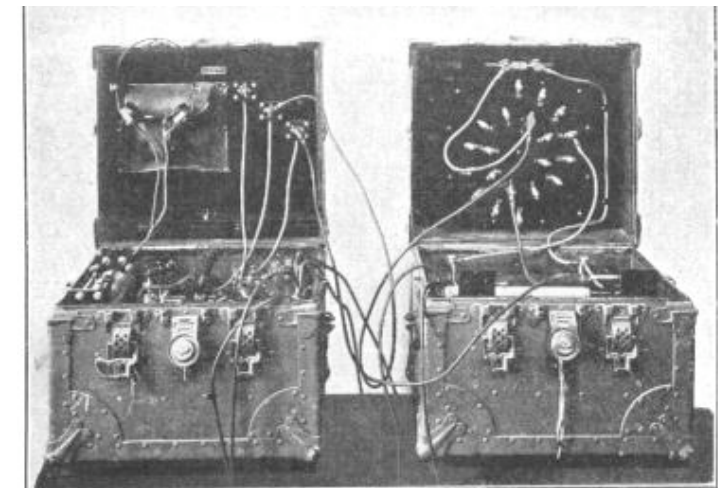


Fig. 108.—U. S. Signal Corps pack sets shown open and closed. Receiving apparatus on the left.

Introduction

The History of Mobile Radio (III)



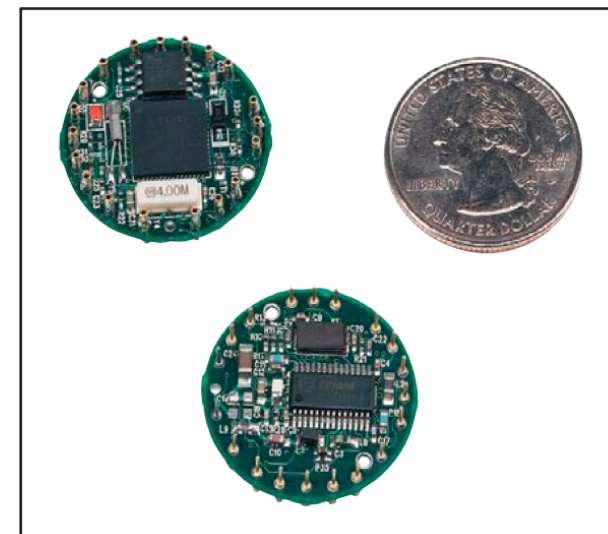
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- 1970s Vint Cerfs Stanford Research Institute (SRI) Van
 - First mobile packet radio traneivers

➤ ...

- 2000s Wireless sensor coin sized sensor nodes Mica2dot from California based Crossbow company



Mobility in Wireless Networks



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Wireless Networks in a Nutshell

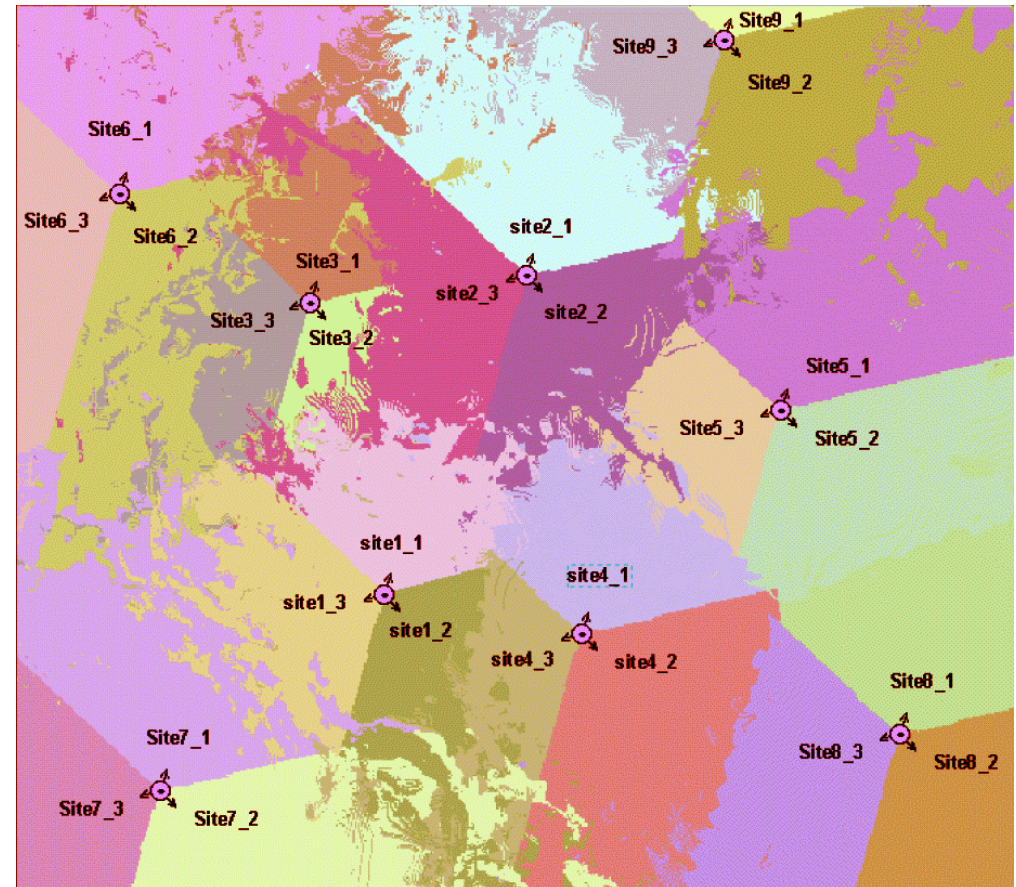
Cellular Networks



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- Static base stations
 - divide the field into cells
- All radio communication is only
 - between base station and client
 - between base stations
 - usually hardwired
- Mobility:
 - movement into or out off a cell
 - sometimes cell sizes vary dynamically (depending on the number of clients - UMTS)
- Main problems:
 - Cellular Handoff
 - Location Service



Wireless Networks in a Nutshell

Mobile Ad Hoc Networks



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➤ MANET:

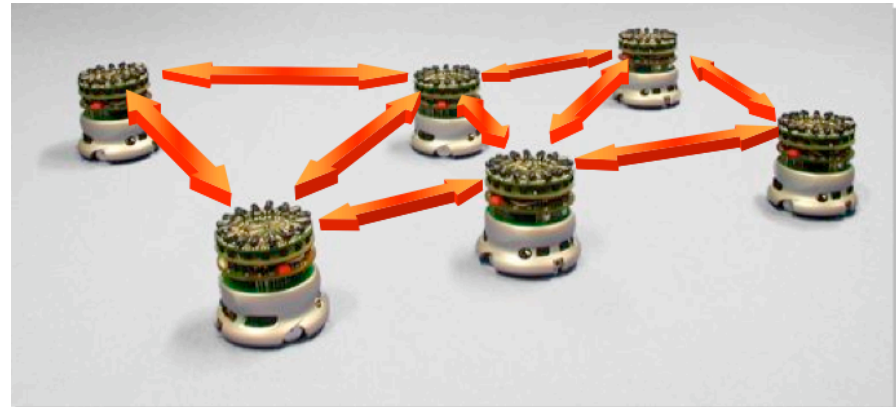
- self-configuring network of mobile nodes
- nodes are routers and clients
- no static infrastructure
- network adapts to changes induced by movement

➤ Positions of clients

- in most applications not available
- exceptions exist

➤ Problems:

- Find a multi-hop route between message source and target
- Multicast a message
- Uphold the network routing tables



Wireless Networks in a Nutshell

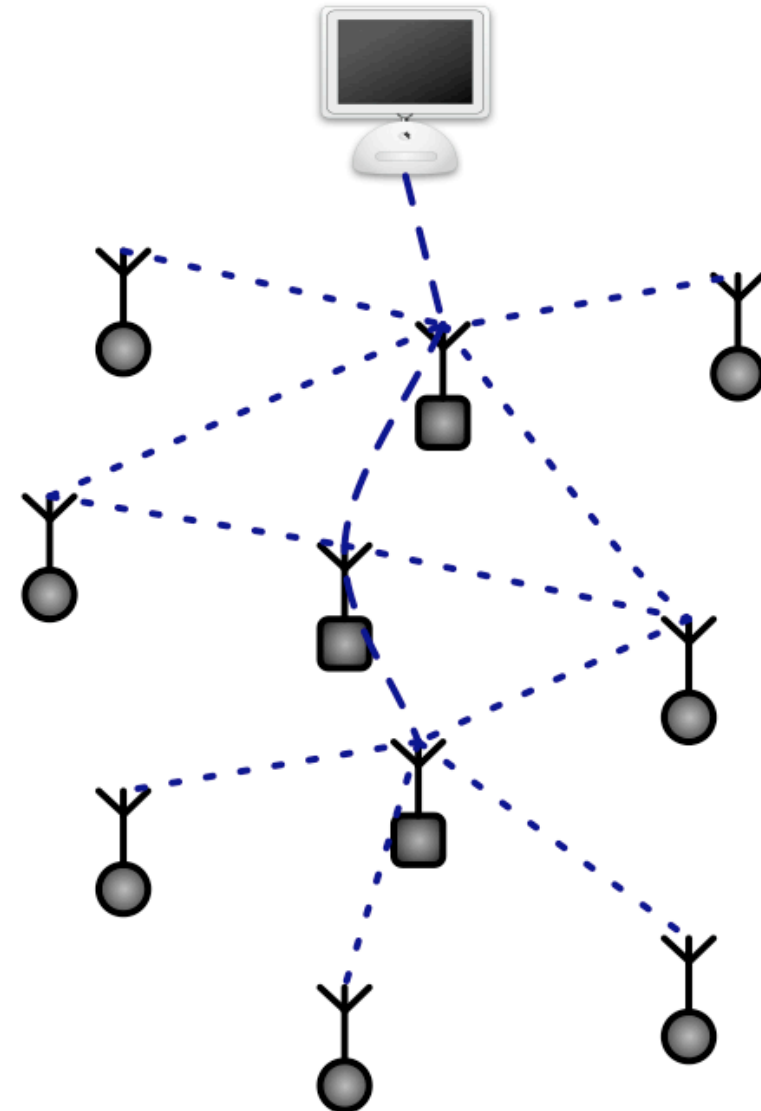
Wireless Sensor Networks



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- Sensor nodes
 - spacially distributed
 - equipped with sensors for
 - temperature, vibration, pressure, sound, motion, ...
- Base stations
 - for collecting the information and control
 - possibly connected by ad-hoc-network
- Main task
 - Read out the sensor information from the field
- Main problem
 - Energy consumption
 - nodes are sleeping most of the time



Mobility in Wireless Networks



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Mobility Patterns: Pedestrian



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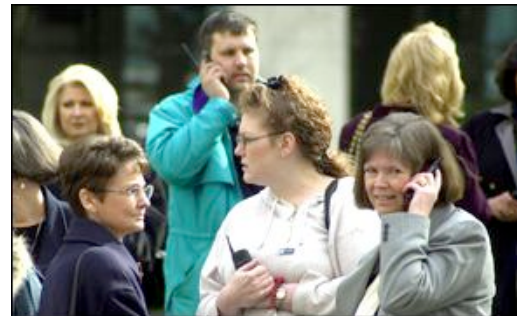
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➤ Characteristics:

- Slow velocity
- Dynamics from obstacles obstructing the signal
 - signal change a matter of meters
- Applies for people or animals
- Complete use of two-dimensional plane
- Chaotic structure
- Possible group behavior
- Limited energy resources

➤ Examples

- Pedestrians on the street or the mall
- Wild life monitoring of animals
- Radio devices for pets



Mobility Patterns: Marine and Submarine



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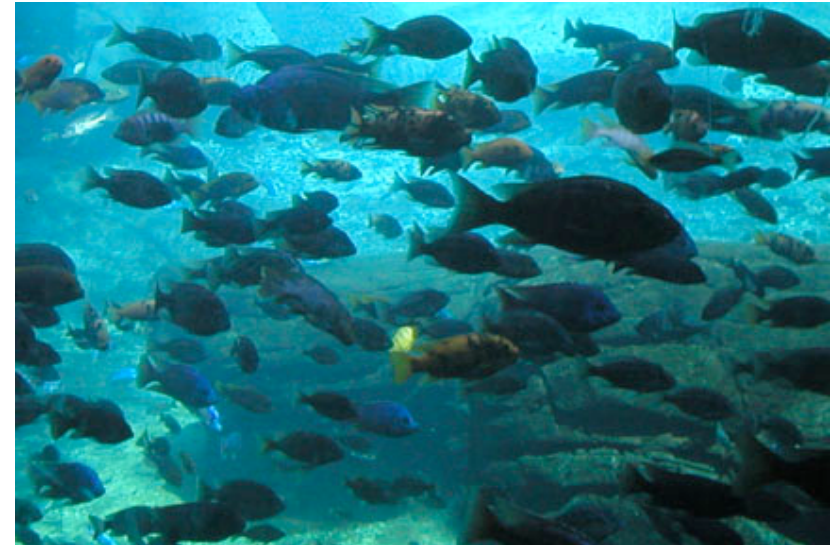
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➤ Characteristics

- Speed is limited due to friction
- Two-dimensional motion
 - submarine: nearly three-dimensional
- Usually no group mobility
 - except conoys, fleets, regattas, fish swarms

➤ Radio communication

- On the water: nearly optimal
- Under the water: terrible
 - solution: long frequencies or sound



Mobility Patterns: Earth bound vehicles

- Mobility by wheels
 - Cars, railways, bicycles, motor bikes etc.
- Features
 - More speed than pedestrians
 - Nearly 1-dimensional mobility
 - because of collisions
 - Extreme group behavior
 - e.g. passengers in trains
- Radio communication
 - Reflections of environment reduce the signal strengths dramatically
 - even of vehicles heading towards the same direction



Mobility Patterns: Aerial Mobility



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➤ Examples:

- Flying patterns of migratory birds
- Air planes

➤ Characteristics

- High speeds
- Long distance travel
 - problem: signal fading
- No group mobility
 - except bird swarms
- Movement two-dimensional
 - except air combat

➤ Application

- Collision avoidance
- Air traffic control
- Bird tracking



Mobility Patterns: Medium Based



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➤ Examples:

- Dropwindsondes in tornadoes/hurricanes
- Drifting buoies

➤ Characteristics of mobility

- Determined by the medium
- Modelled by Navier-Stokes-equations
- Medium can be 1,2,3-dimensional
- Group mobility may occur
 - is unwanted, because no information
- Location information is always available
 - this is the main purpose



Mobility Patterns: Outer Space



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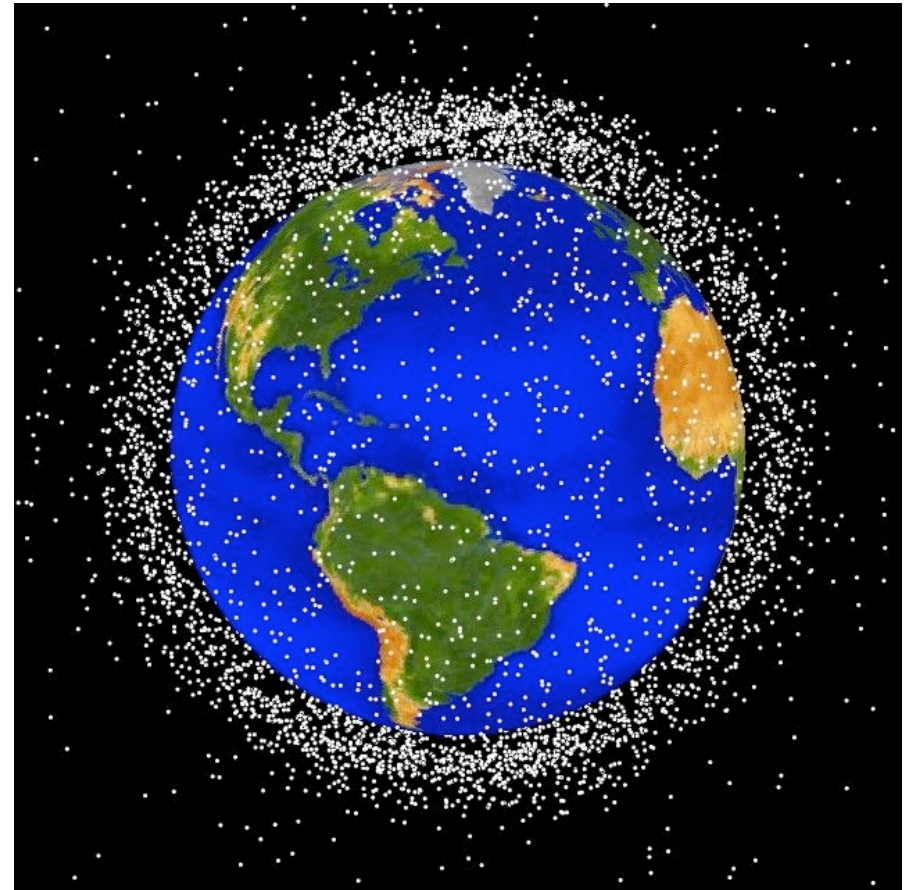
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➤ Characterization

- Acceleration is the main restriction
- Fuel is limited
- Space vehicles drift through space most of the time
- Non-circular orbits possible
- Mobility in two-planet system is chaotic
- Group behavior in future systems

➤ Radio communication

- Perfect signal transmission
- Energy supply usually no problem (solar paddles)



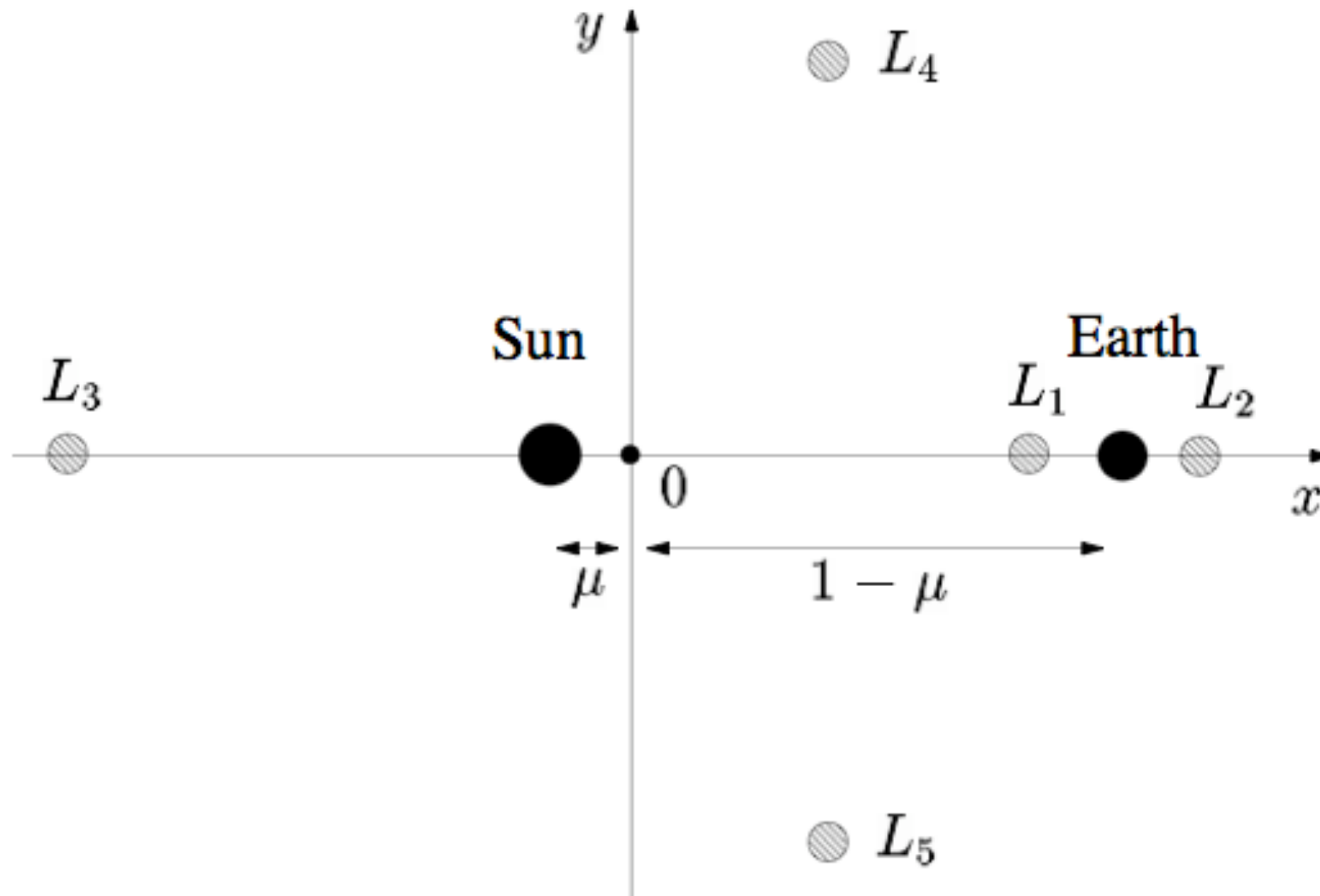
Mobility Patterns

Outer Space: Chaotic Mobility



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Mobility Patterns

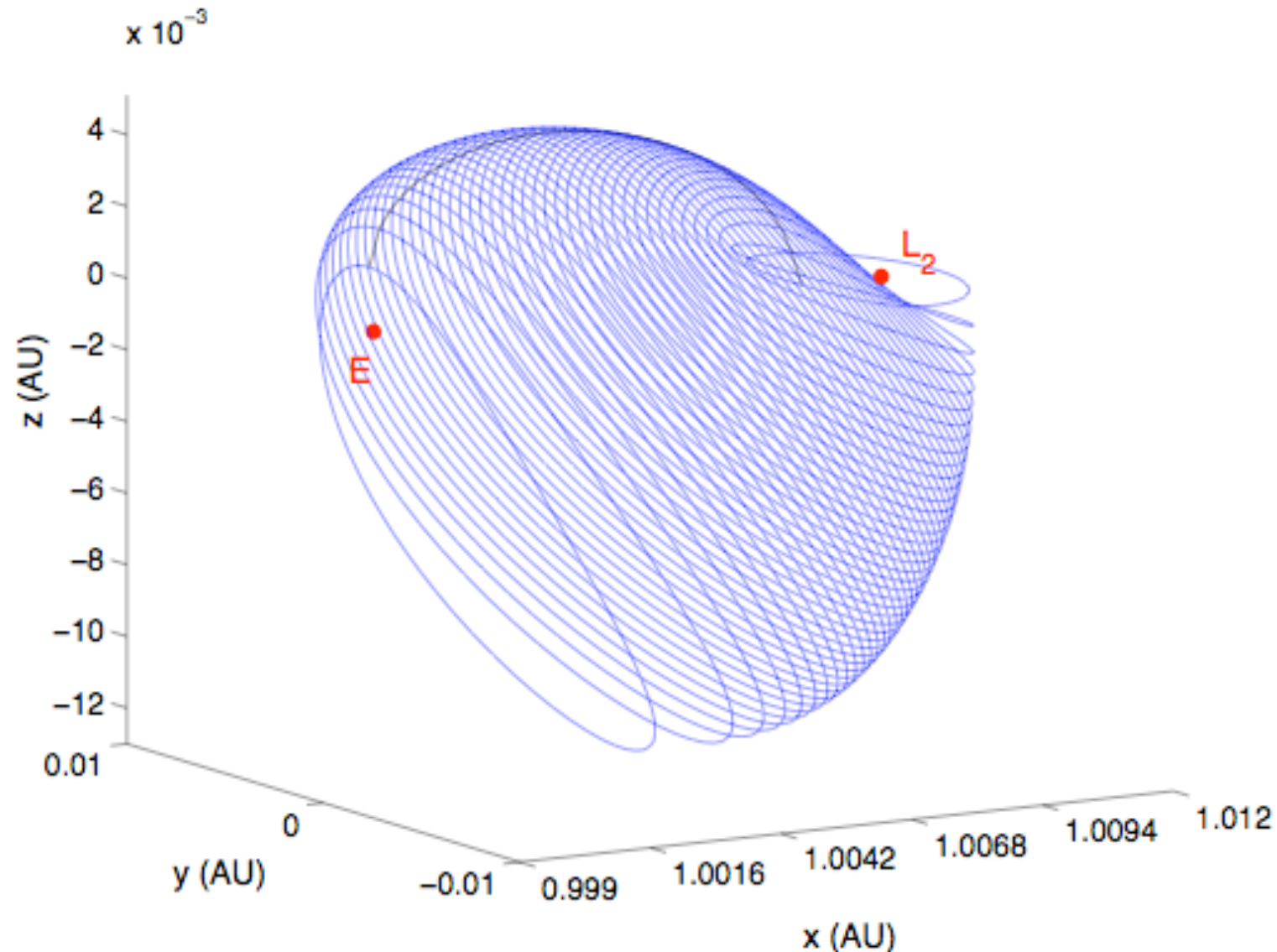
Outer Space: Chaotic Mobility

[Junge et al. 2002]



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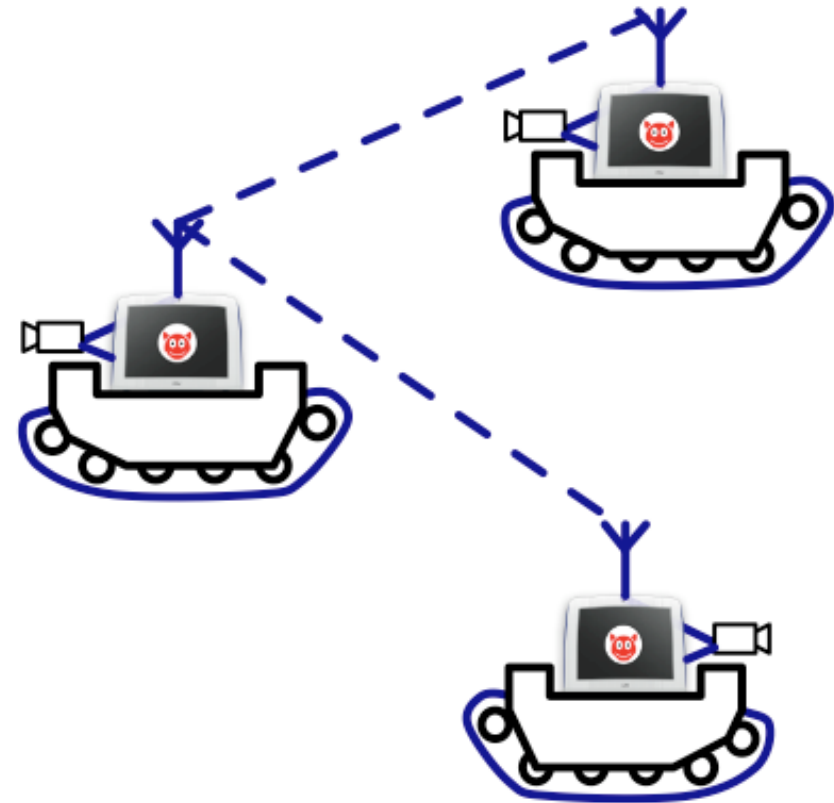
Mobility Patterns: Robot Motion



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- Scenario
 - any above
- Main difference
 - Mobility behavior given by the programmer
- Predictability?
 - depends on programmer and environment
- Problem
 - Robot motion designer don't care about communication
 - Robot goals and wireless communication may conflict
- Solution
 - Find a compromise
 - “Smart Team Project”



Mobility Patterns: Characterization



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- Group behavior
 - Can be exploited for radio communication
- Limitations
 - Speed
 - Acceleration
- Dimensions
 - 1, 1^{1/2}, 2, 2^{1/2}, 3
- Predictability
 - Simulation model
 - Completely erratic
 - Described by random process
 - Deterministic (selfish) behavior

Mobility Patterns: Measuring Mobility



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- How to measure mobility?
 - Use a wireless sensor network!
- Localization in wireless networks
 - Signal strength
 - Time of arrival
 - Time difference of arrival
 - Angle of arrival
 - Hop count based techniques
 - Cell information
- Global Positioning System (GPS)
 - (predecessor of Galileo)
 - Works very well on the planet's surface
 - Perfect for cars, trucks, trains, bikes, pets, cows, zebras,...
 - Not in offices, shopping malls, subway systems, tunnels, underwater
 - Not always available
 - Energy consumption, cost, distances too short

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Models of Mobility

Cellular Mobility



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➤ Random Walk

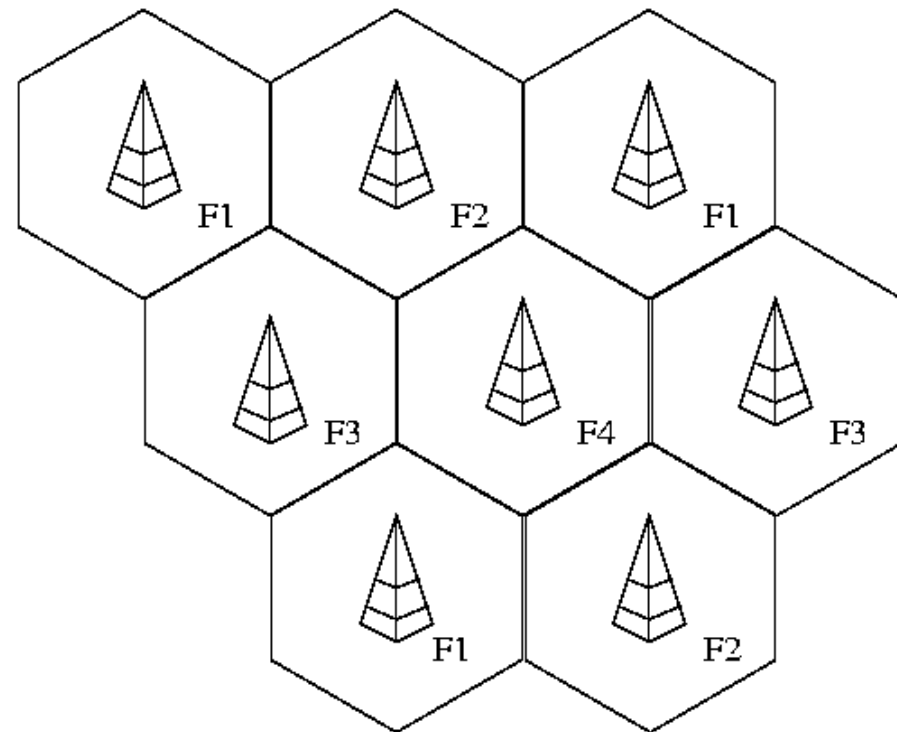
- A node stays in a cell or changes to a neighbored cell with a given probability
- Memoryless model for handoff

➤ Trace Based

- Large records of real mobility patterns of users
- Simulate handoff

➤ Fluid Flow

- Macroscopic level
- Mobility is modeled like a fluid/gas in a pipe
- works very well for highways
- insufficient for individual movements including stopping and starting



Models of Mobility

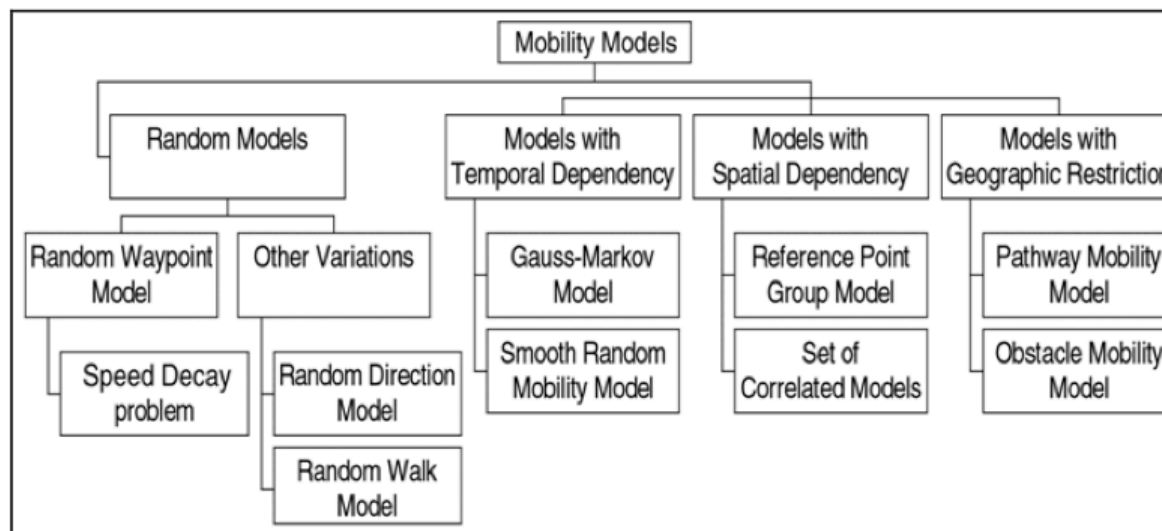
Random Trip Mobility



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- Random Walk
- Random Waypoint
- Random Direction
- Boundless Simulation Area
- Gauss-Markov
- Probabilistic Version of the Random Walk Mobility
- City Section Mobility Model



[Bai and Helmy in
Wireless Ad Hoc
Networks 2003]

Models of Mobility

Brownian Motion, Random Walk

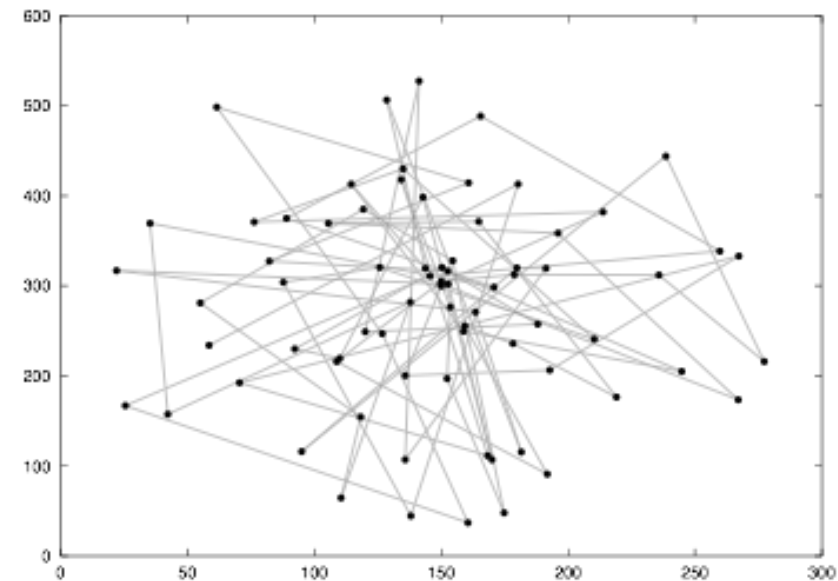


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- Brownian Motion (microscopic view)
 - speed and direction are chosen randomly in each time step (uniformly from $[v_{\min}, v_{\max}]$ and $[0, \pi]$)

- Random Walk
 - macroscopic view
 - memoryless
 - e.g., for cellular networks
 - movement from cell to cell
 - choose the next cell randomly
 - residual probability



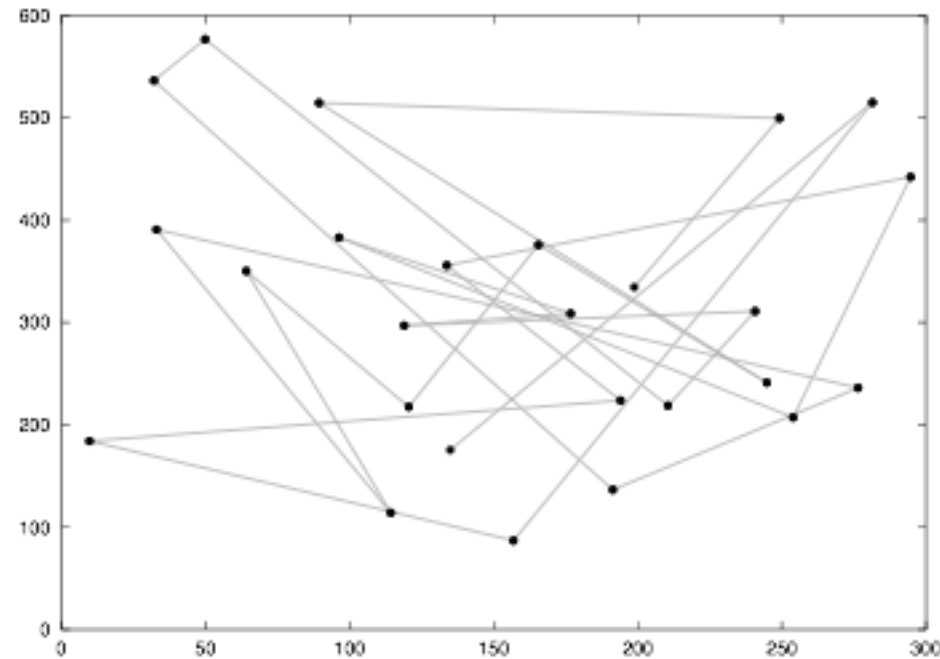
[Camp et al. 2002]

Models of Mobility

Random Waypoint Mobility Model

[Johnson, Maltz 1996]

- move directly to a randomly chosen destination
- choose speed uniformly from $[v_{\min}, v_{\max}]$
- stay at the destination for a predefined pause time



[Camp et al. 2002]



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Models of Mobility

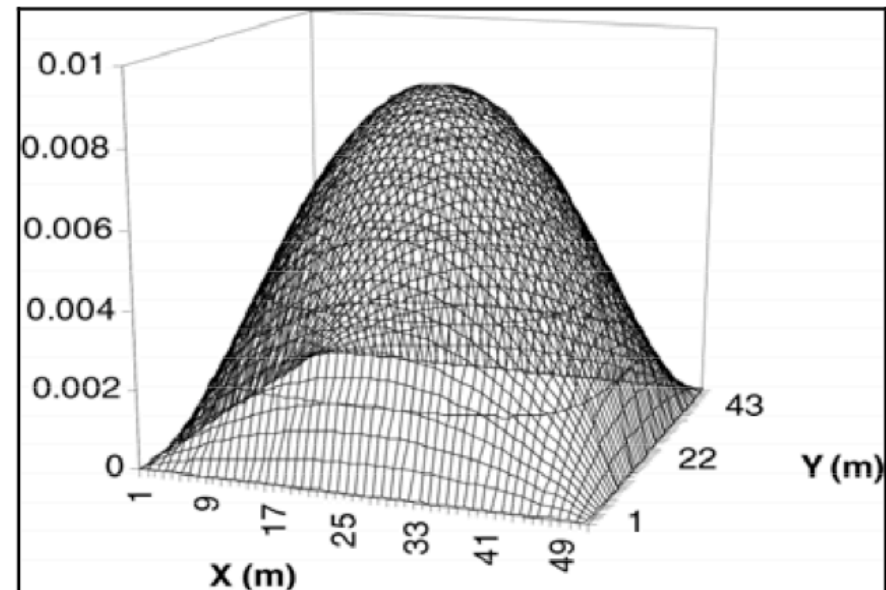
Problems of Random Waypoint



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- In the limit not all positions occur with the same probability
- If the start positions are uniformly at random
 - then the transient nature of the probability space changes the simulation results
- Solution:
 - Start according the final spatial probability distribution



Models of Mobility

Gauss-Markov Mobility Model

[Liang, Haas 1999]



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➤ adjustable degree of randomness

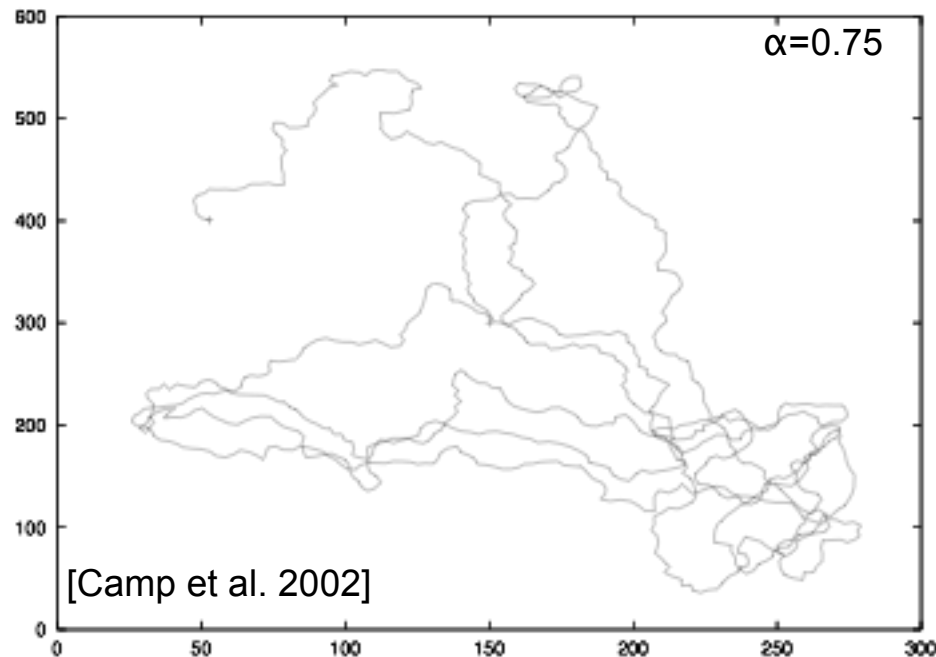
➤ velocity: $v_n = \alpha v_{n-1} + (1 - \alpha)\bar{v} + \sqrt{1 - \alpha^2}v_{X_{n-1}}$

➤ direction: $d_n = \alpha d_{n-1} + (1 - \alpha)\bar{d} + \sqrt{1 - \alpha^2}d_{X_{n-1}}$

↑
tuning factor

↑
mean

↑
random variable
gaussian distribution



Models of Mobility

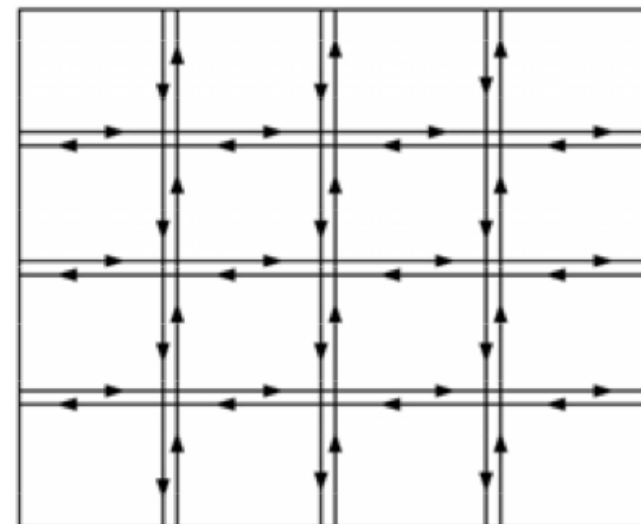
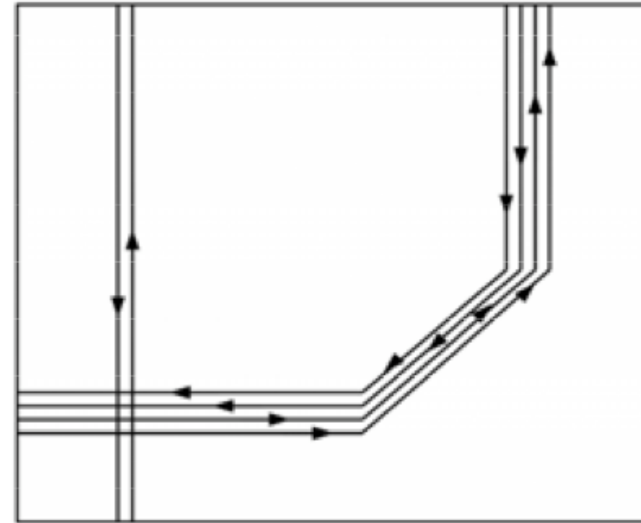
City Section and Pathway



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- Mobility is restricted to pathways
 - Highways
 - Streets
- Combined with other mobility models like
 - Random walk
 - Random waypoint
 - Trace based
- The path is determined by the shortest path between the nearest source and target



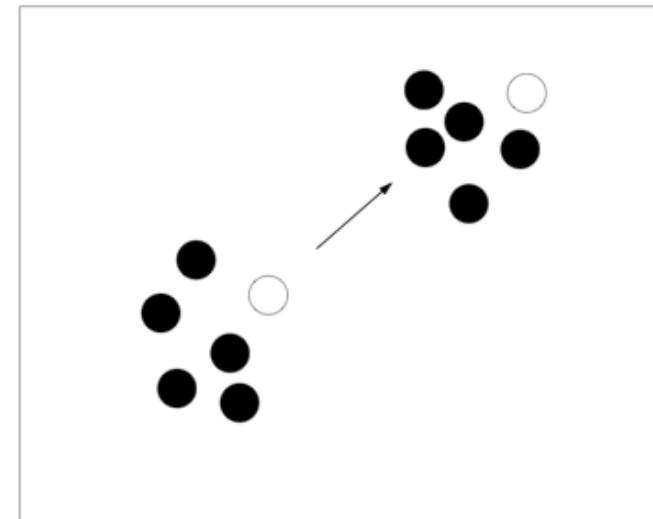
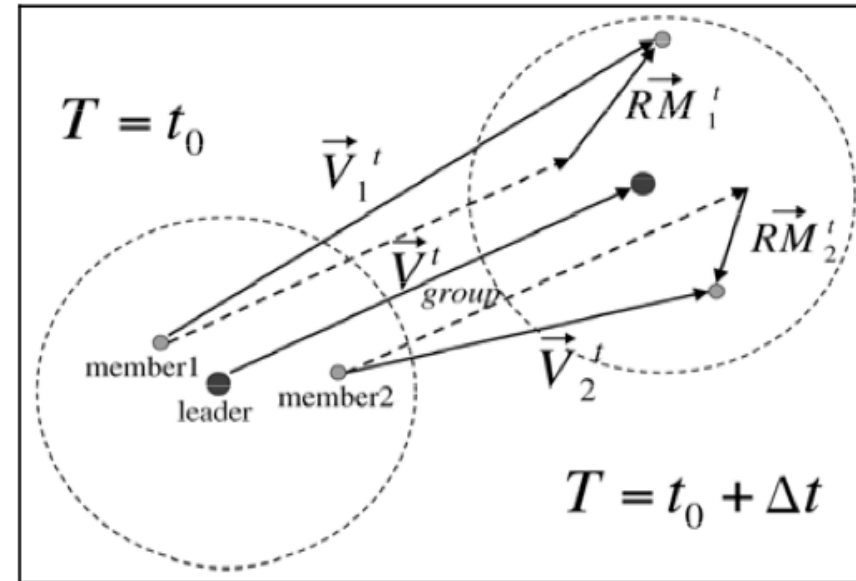
Models of Mobility: Group-Mobility Models



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- Exponential Correlated Random
 - Motion function with random deviation creates group behavior
- Column Mobility
 - Group advances in a column
 - e.g. mine searching
- Reference Point Group
 - Nomadic Community Mobility
 - reference point of each node is determined based on the general movement of this group with some offset
 - Pursue Mobility
 - group follows a leader with some offset



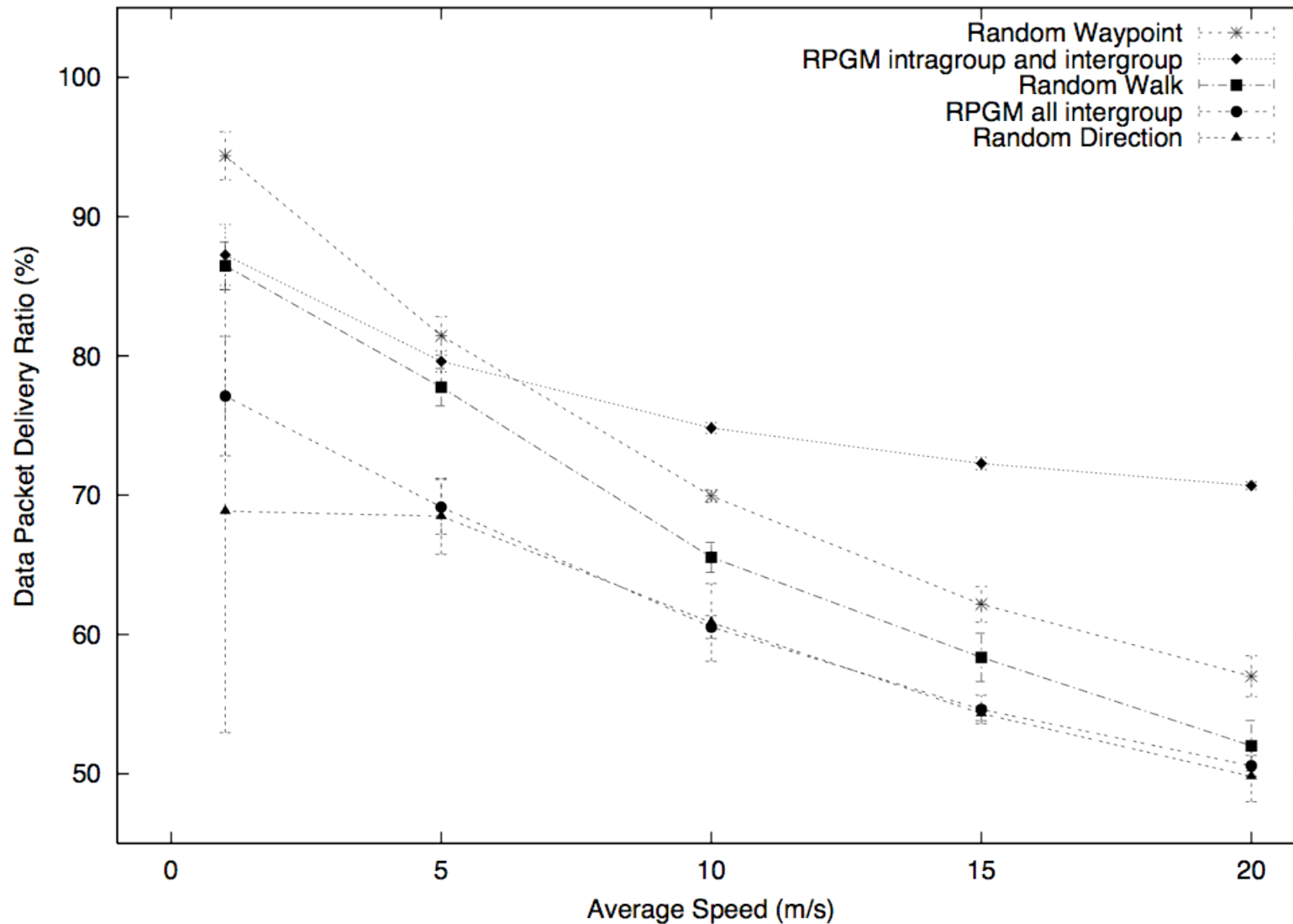
Models of Mobility



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➤ The influence of the type of mobility is enormous



Models of Mobility

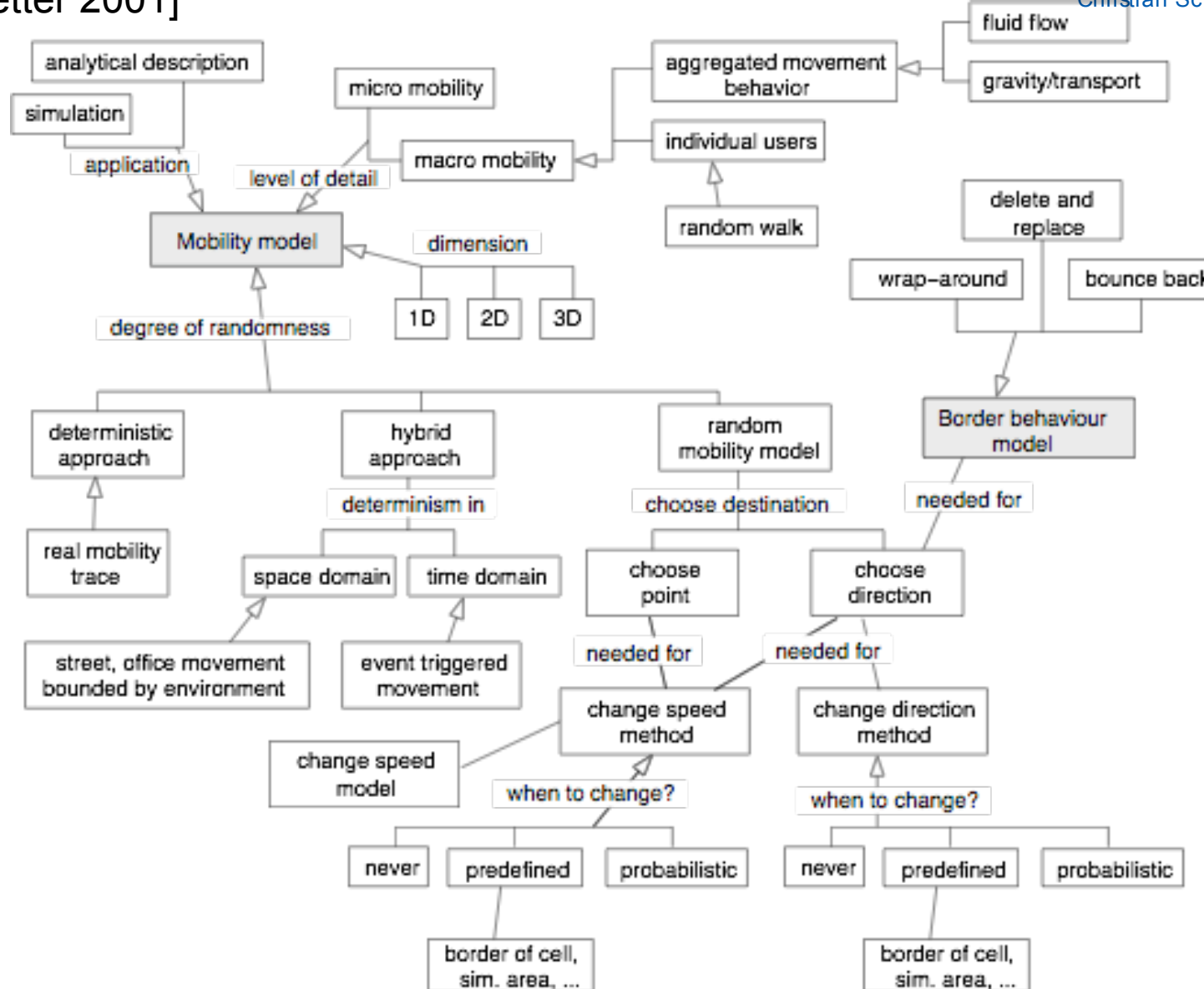
Combined Mobility Models

[Bettstetter 2001]



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Models of Mobility: Non-Recurrent Models

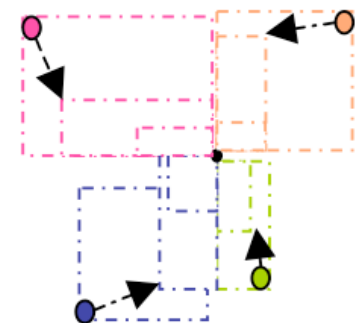
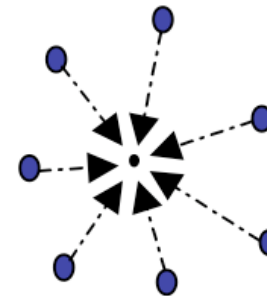
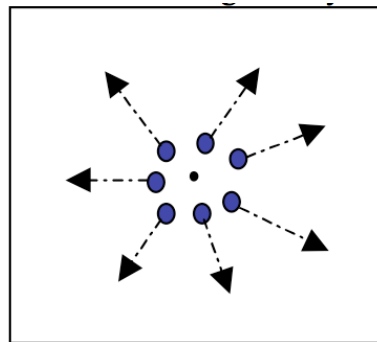


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- Kinetic data structures (KDS)
 - framework for analyzing algorithms on mobile objects
 - mobility of objects is described by pseudo-algebraic functions of time.
 - analysis of a KDS is done by counting the combinatorial changes of the geometric structure
- Usually the underlying trajectories of the points are described by polynomials
 - In the limit points leave the scenario
- Other models [Lu, Lin, Gu, Helmy 2004]
 - Contraction models
 - Expansion models
 - Circling models

This room is for rent.



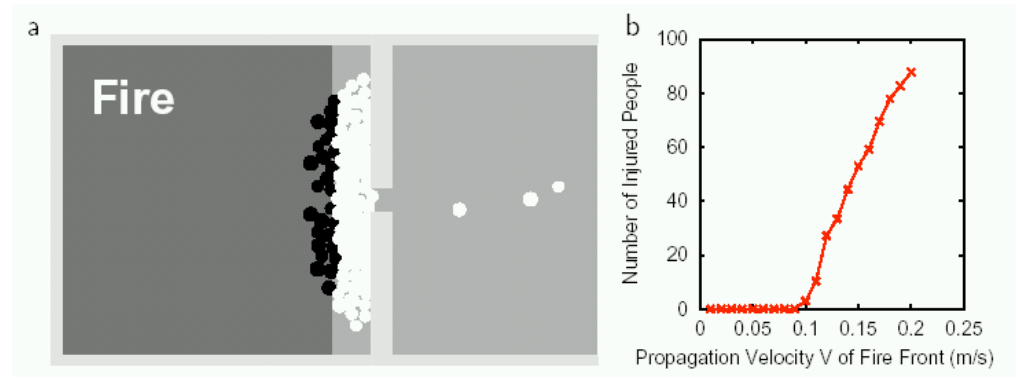
Models of Mobility: Particle Based Mobility



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- Motivated by research on mass behavior in emergency situations
 - Why do people die in mass panics?
- Approach of [Helbing et al. 2000]
 - Persons are models as particles in a force model
 - Distinguishes different motivations and different behavior
 - Normal and panic



Models of Mobility:

Particle Based Mobility: Pedestrians



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➤ Speed:

- f : sum of all forces
- ξ : individual fluctuations

$$v_i(t) := \frac{dx_i(t)}{dt}$$

$$m_i \cdot \frac{dv_i(t)}{dt} = f_i(t) + \xi_i(t) ,$$

➤ Target force:

- Wanted speed v^0 and direction e^0

$$\frac{v_i^0 e_i^0 - v_i(t)}{\tau_i}$$

➤ Social territorial force

$$f_{ij}^{soc}(t) = A_i e^{\frac{r_{ij}-d_{ij}}{B_i}} n_{ij} \left(\lambda_i + (1 - \lambda_i) \frac{1 + \cos(\phi_{ij})}{2} \right)$$

➤ Attraction force (shoe store)

$$f_{ij}^{att}(t) = -C_i n_{ij}$$

$$n_{ij}(t) = \frac{x_i(t) - x_j(t)}{d_{ij}(t)}$$

➤ Pedestrian force (overall):

$$f_i(t) = \frac{v_i^0(t)e_i^0(t) - v_i(t)}{\tau_i} + \sum_{j \neq i} f_{ij}^{soc}(t) + \sum_{j \neq i} f_{ij}^{att}(t) + \sum_k f_{ij}^{att}(t) + \sum_b f_{ib}^{obst}(t)$$

Models of Mobility:

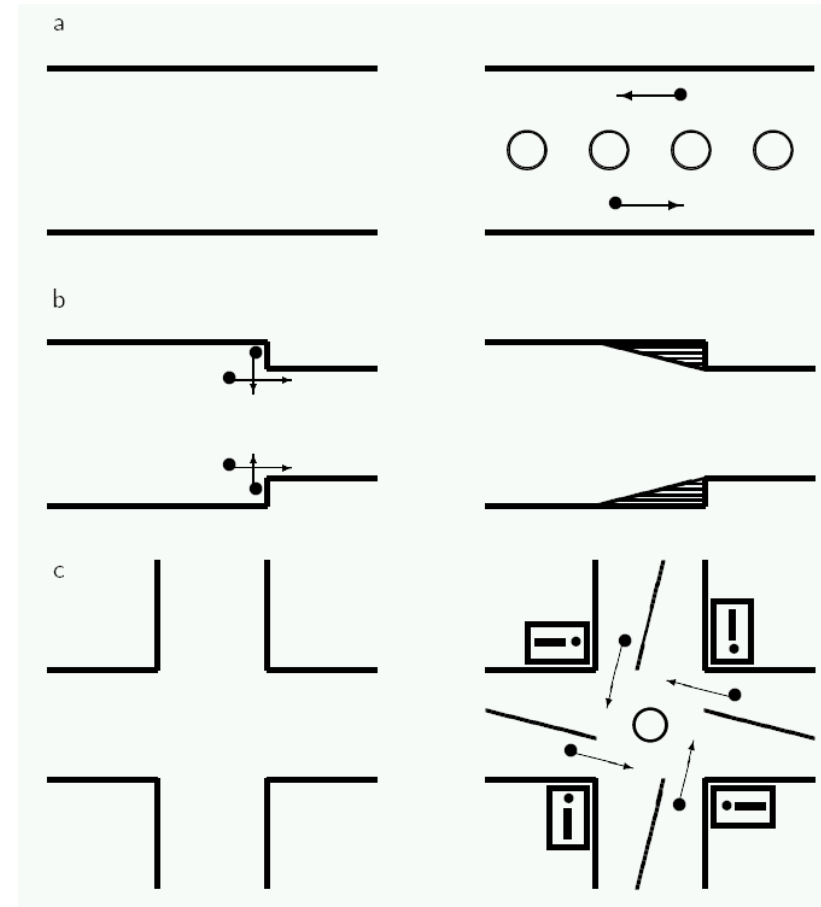
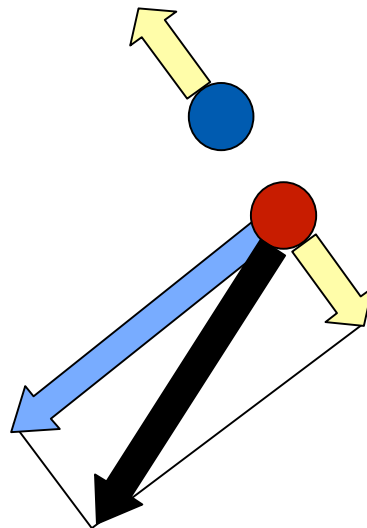
Particle Based Mobility: Pedestrians



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- This particle based approach predicts the reality very well
 - Can be used to design panic-safe areas
- Bottom line:
 - All persons behave like mindless particles



Models of Mobility

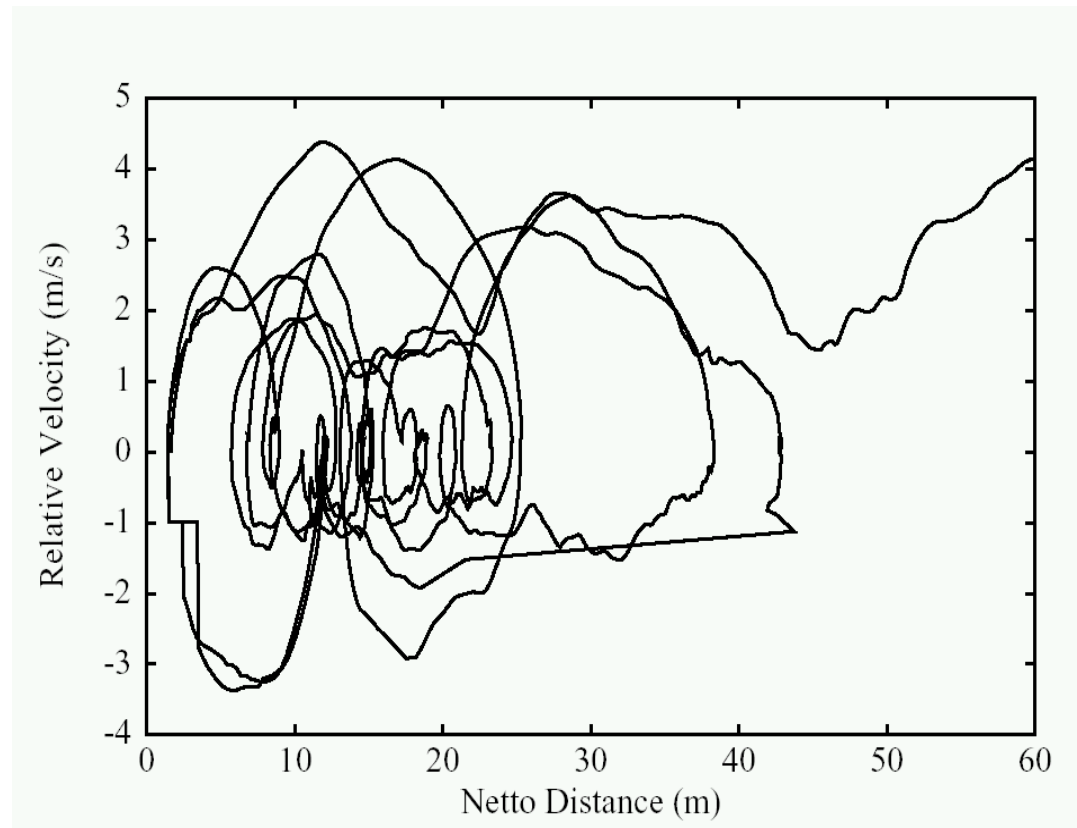
Particle Based Mobility: Vehicles



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- Vehicles use 1-dimensional space
- Given
 - relative distance to the predecessor
 - relative speed to the predecessor
- Determine
 - Change of speed



Models of Mobility:

Particle Based Mobility: Pedestrians



- Similar as in the pedestrian model

$$\frac{dv_i(t)}{dt} = f_i^0(t) + \sum_{j \neq i} f_{ij}(x_i(t), v_i(t), x_j(t), v_j(t)) + \xi_i(t)$$

- Each driver watches only the car in front of him
- No fluctuation

$$\frac{dv_i(t)}{dt} = f_i^0(t) + f_{i,i-1}(x_i(t), v_i(t), x_{i-1}(t), v_{i-1}(t))$$

- $s(v_i) = d_i + T_i v_i$, d_i is minimal car distance, T_i is security distance
- $h(x) = x$, if $x > 0$ and 0 else, R_i is break factor
- $s_i(t) = (x_i(t) - x_{i-1}(t))$ - vehicle length
- $\Delta v_i = v_i - v_{i-1}$

$$f_{i,i-1} = \frac{V_i(t) - v_i^0}{\tau_i} - \frac{\Delta v_i h(\Delta v_i)}{\tau_i'} e^{\frac{s_i(t) - s(v_i)}{R_i'}}$$

- where

$$V_i(t) = v_i^0 \left(1 - e^{-\frac{s_i(t) - s(v_i(t))}{R_i}} \right)$$

Models of Mobility

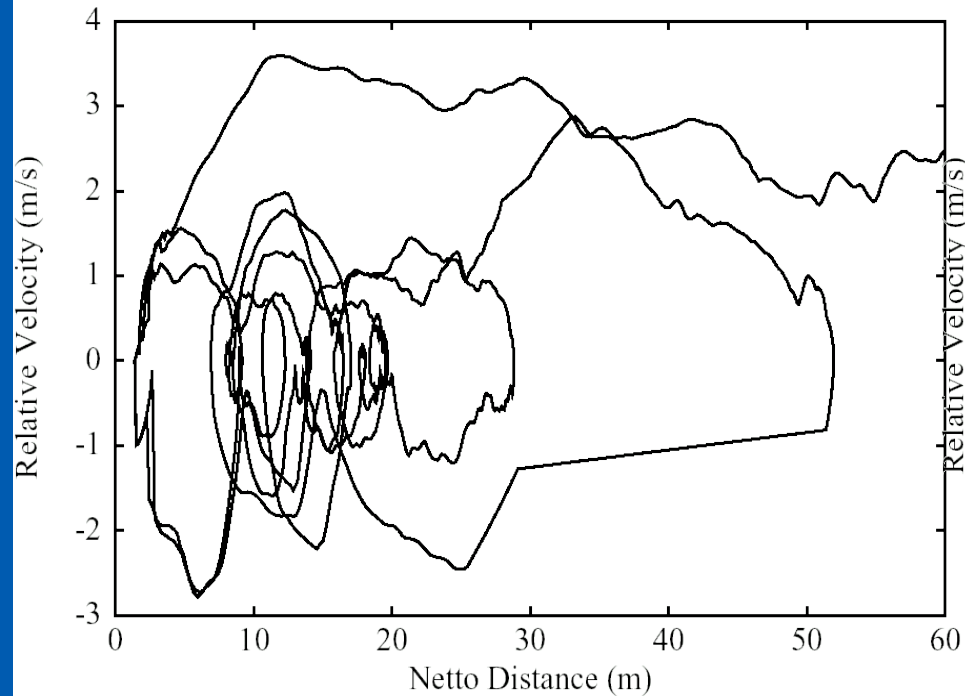
Particle Based Mobility: Vehicles



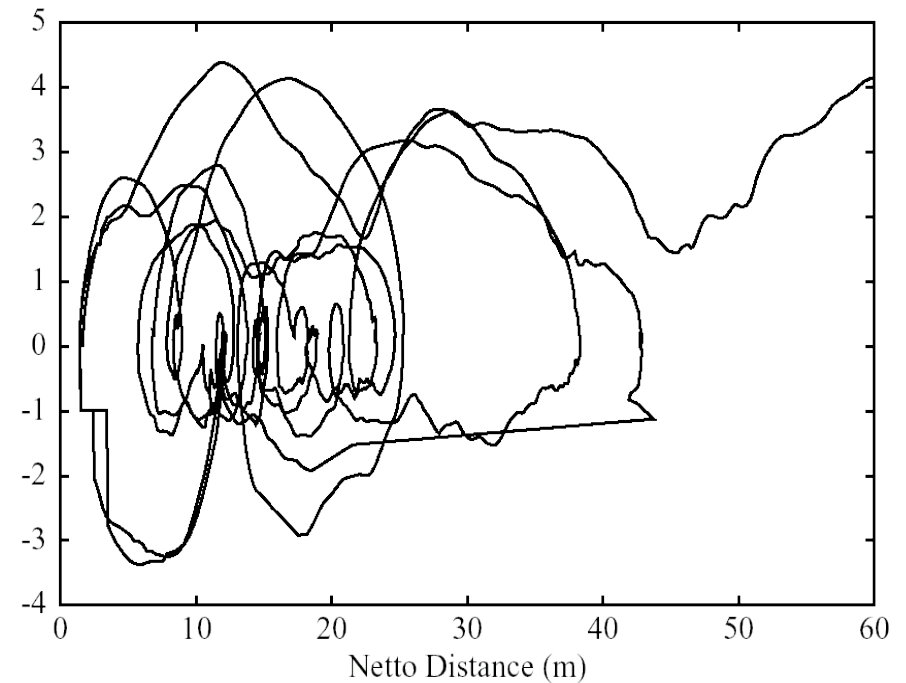
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Reality



**Simulation
with GFM**



Modeling Worst Case Mobility

[S., Lukovszki, Rührup, Volbert 2003]



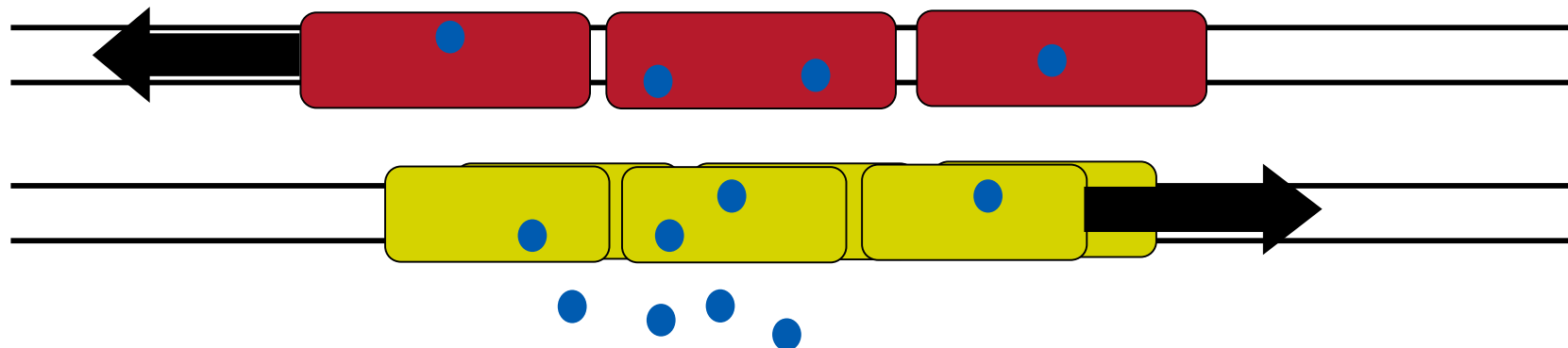
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V: Pedestrian Model \leftrightarrow Maximum velocity $\leq v_{\max}$



A: Vehicular Model \leftrightarrow Maximum acceleration $\leq a_{\max}$



Modeling Worst Case Mobility



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- Synchronous round model
- In every round of duration Δ
 - Determine positions (speed vectors) of possible comm. partners
 - Establish (stable) communication links
 - Update routing information
 - Do the job, i.e. packet delivery, live video streams, telephone,...

Modeling

Worst Case Mobility: Crowds



- Crowdedness of node set
 - natural lower bound on network parameters (like diversity)

1. Pedestrian (v) model:

- Maximum number of nodes that can collide with a given node in time span $[0, \Delta]$

$$\text{crowd}_v(u) := \# \{w \in S \setminus \{u\} : |u - w|_2 \leq 2v_{\max}\Delta\}$$

2. Vehicular (a) model:

- Maximum number of nodes that may move to node u meeting it with zero relative speed in time span $[0, \Delta]$

$$\text{crowd}_a(u) := \# \left\{ w \in S \setminus \{u\} : |u - w|_2 \leq \frac{1}{2}a_{\max}\Delta^2 \text{ and } |u' - w'|_2 \leq \frac{1}{2}a_{\max}\Delta \right\}$$

- $\text{crowd}(S) := \max_{u \in S} \text{crowd}(u)$

Modeling - Worst Case Mobility: Transmission Range of Pedestrian Communication

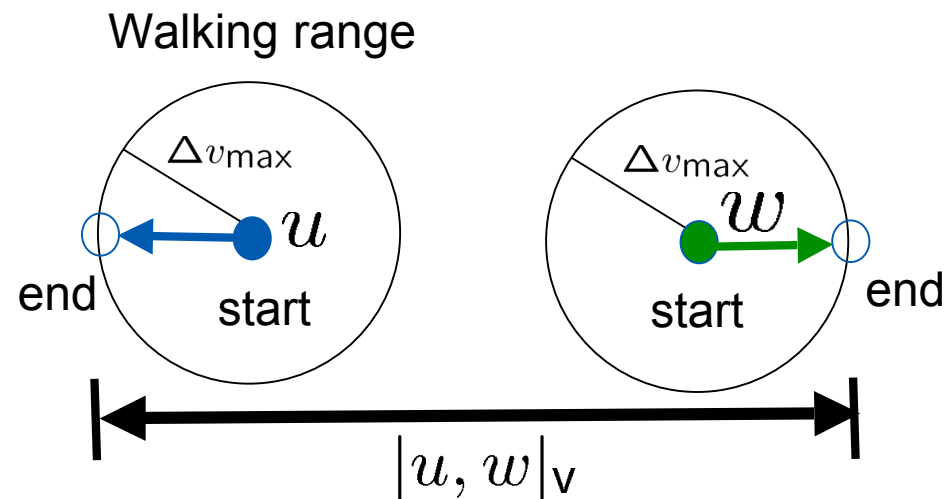


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➤ Pedestrian model / Velocity bounded model

$$|u, w|_v := 2\Delta v_{\max} + |u - w|_2$$



Modeling - Worst Case Mobility Transmission Range of Vehicular Communication

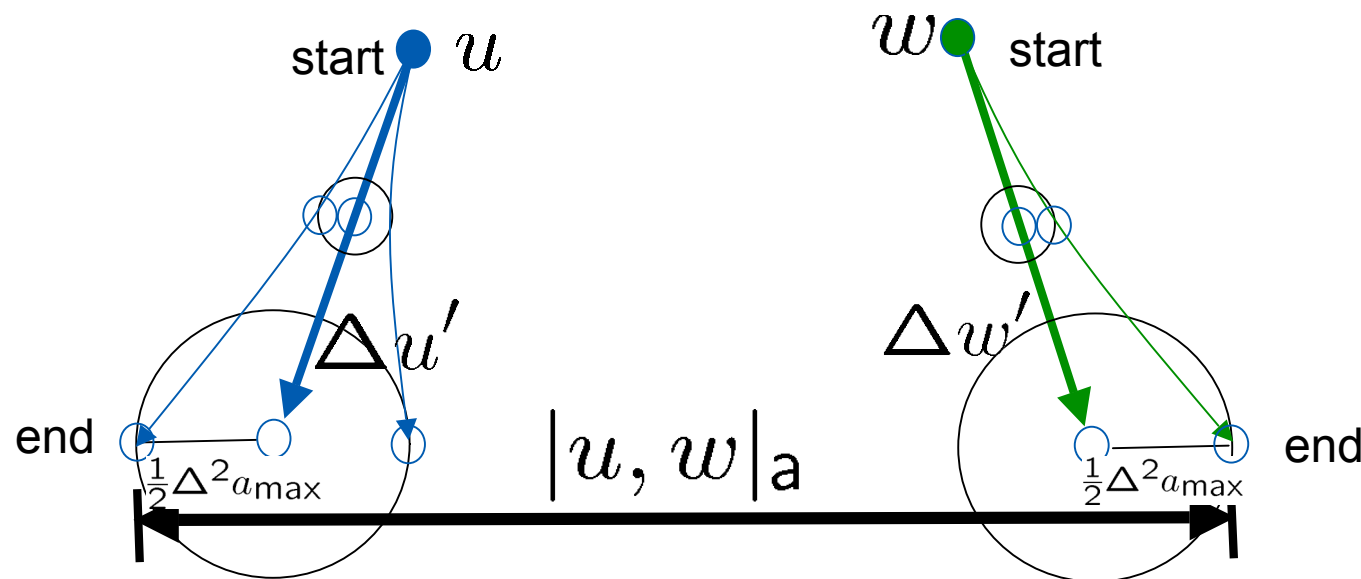


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➤ Vehicular mobility model / Acceleration bounded model

$$|u, w|_a := \max\{|u-w|_2, |u-w+(u'-w')\Delta|_2 + a_{\max}\Delta^2\}$$



Modeling - Worst Case Mobility

Mobile Radio Interferences



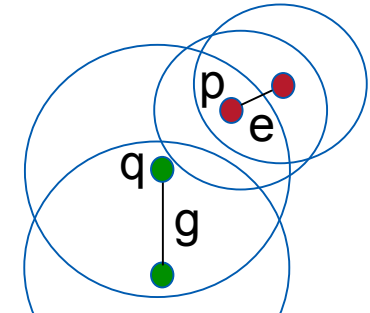
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An edge g interferes with edge e in the

1. Pedestrian (v) model

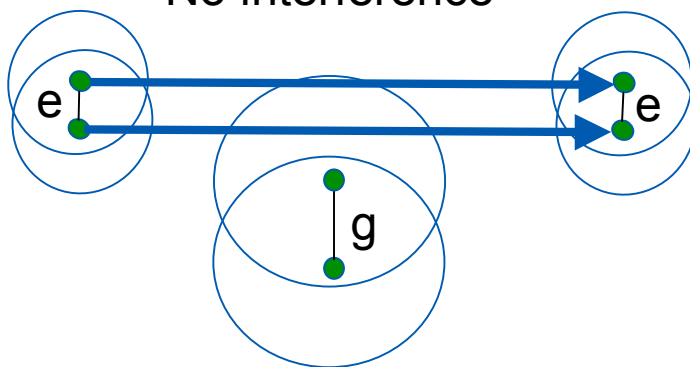
$$g \in \text{Int}_v(e) \iff \exists p \in e, \exists q \in g : |p - q|_2 \leq |g|_v$$



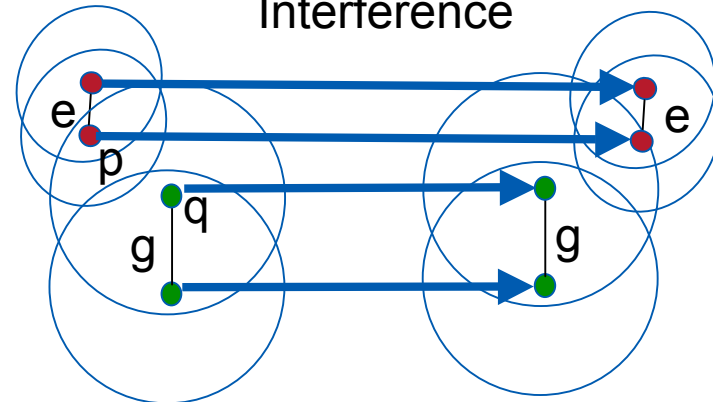
2. Vehicular (a) model

$$g \in \text{Int}_a(e) \iff \exists p \in e, \exists q \in g : |p - q|_2 \leq |g|_a \text{ and } |p - q + \Delta(p' - q')|_2 \leq |g|_a$$

No interference



Interference





Theorem

In both mobility models we observe for all connected graphs G :

$$\text{Int}(G) \geq \text{crowd}(S) - 1$$

Lemma

In both mobility models $\alpha \in \{v, a\}$ every mobile spanner is also a mobile power spanner, i.e. for some $\beta \geq 1$ for all $u, w \in S$ there exists a path $(u=p_0, p_1, \dots, p_k=w)$ in G such that:

$$\sum_{i=1}^k (|p_{i-1}, p_i|_\alpha)^\beta \leq c \cdot (|u, w|_\alpha)^\beta$$



Theorem

Given a mobile spanner G for any of our mobility models then

- for every path system \mathcal{P} in a complete network C
- there exists a path system \mathcal{P}' in G such that

$$C_{\mathcal{P}'}(G) := \mathcal{O}(C_{\mathcal{P}}(G) \cdot \text{Int}(G) \cdot \log n)$$

Theorem

The Hierarchical Grid Graph constitutes a mobile spanner with at most $\mathcal{O}(\text{crowd}(V) + \log n)$ interferences (for both mobility models).

The Hierarchical Grid Graph can be built up in $\mathcal{O}(\text{crowd}(V) + \log n)$ parallel steps using radio communication

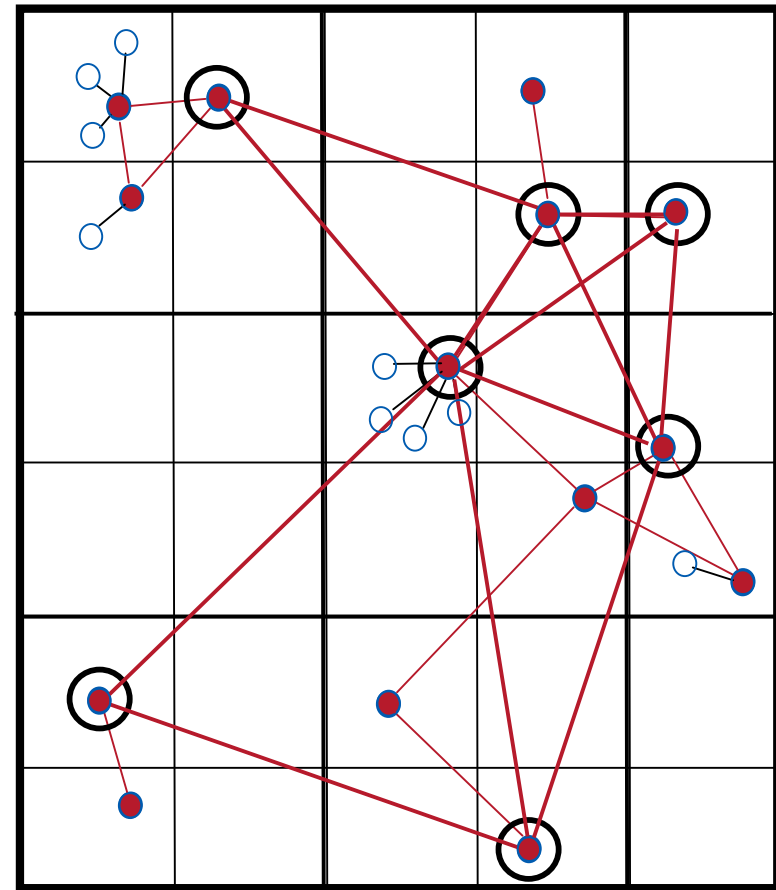
Modeling - Worst Case Mobility: Hierarchical Grid Graph (pedestrians)



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- Start with grid of box size Δv_{\max}
- For $O(\log n)$ rounds do
 - Determine a cluster head per box
 - Build up star-connections from all nodes to their cluster heads
 - Erase all non cluster heads
 - Connect neighbored cluster heads
 - Increase box size by factor 2
- od



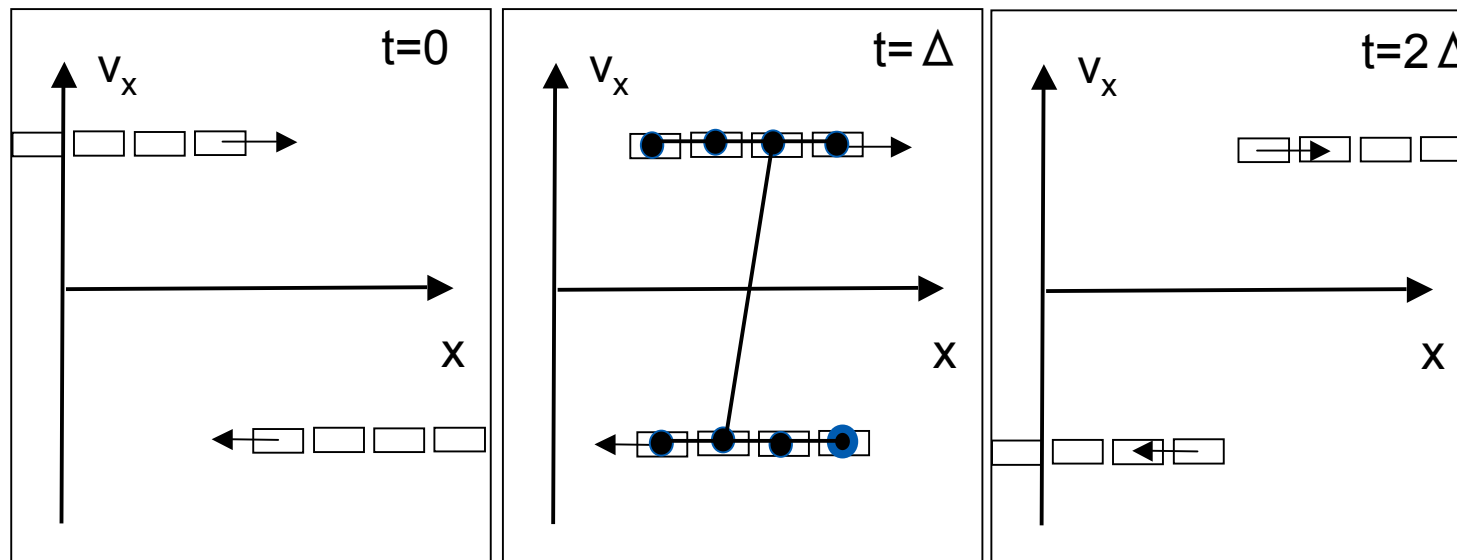
Modeling - Worst Case Mobility: The Hierarchical Grid Graph (vehicular)



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- Algorithm:
 - Consider coordinates $(x(s_i), y(s_i), x(s'_i), y(s'_i))$
 - Start with four-dimensional grid
 - with rectangular boxes of size $(6\Delta^2 a_{\max}, 6\Delta^2 a_{\max}, 2\Delta v_{\max}, 2\Delta v_{\max})$
 - Use the same algorithm as before





Theorem

There exist distributed algorithms that construct a mobile network G for velocity bounded and acceleration bounded model with the following properties:

1. G allows routing approximating the optimal congestion by $O(\log^2 n)$
 2. Energy-optimal routing can be approximated by a factor of $O(1)$
 3. G approximates the minimal interference number by $O(\log n)$
 4. The degree is $O(\text{crowd}(S) + \log n)$
 5. The diameter is $O(\log n)$
- Still no routing can satisfy small congestion and energy at the same time!

Mobility in Wireless Networks



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- Introduction
- Wireless Networks in a Nutshell
 - Cellular Networks
 - Mobile Ad Hoc Networks
 - Sensor Networks
- Mobility Patterns
 - Pedestrian
 - Marine and Submarine
 - Earth bound Vehicles
 - Aerial
 - Medium Based
 - Outer Space
 - Robot Motion
 - Characterization of Mobility Patterns
 - Measuring Mobility Patterns

- Models of Mobility
 - Cellular
 - Random Trip
 - Group
 - Combined
 - Non-Recurrent
 - Particle based
 - Worst Case
- **Discussion**
 - Mobility is Helpful
 - Mobility Models and Reality

Discussion: Mobility is Helpful



- Positive impacts of mobility:
- Improves coverage of wireless sensor networks
- Helps security in ad hoc networks
- Decreases network congestion
 - can overcome the natural lower bound of throughput of $O(\sqrt{n})$
 - mobile nodes relay packets
 - literally transport packets towards the destination node

Discussion: Mobility Models and Reality



- Discrepancy between
 - realistic mobility patterns and
 - benchmark mobility models
- Random trip models
 - prevalent mobility model
 - assume individuals move erratically
 - more realistic adaptations exist
 - really realistic?
 - earth bound or pedestrian mobility in the best case
- Group mobility
 - little known
 - social interaction or physical process?
- Worst case mobility
 - more general
 - gives more general results
 - yet only homogenous participants
 - network performance characterized by crowdedness

Conclusion: What to do?



- It is possible to formulate mobility models for
 - marine
 - aerial
 - medium based
 - outer space mobility patterns
- Improvements can be expected for
 - pedestrian
 - vehicular mobility models
- Research of mobility models
 - at the beginning
- Todo
 - Find mobility models for specific mobility patterns
 - Prove the validity by comparing with reality
 - Prove the efficiency and reliability of real network protocols with respect to the mobility model



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Thanks for your attention!

Mobility in Wireless Networks

Invited Talk for SOFSEM 2006

Mérín, Czech Republic

26th January 2006



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