

A Framework for the Design and Verification of Component-Based Systems

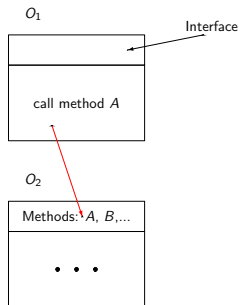
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joint work with G. Gössler, S. Graf, M. Martens, and J. Sifakis

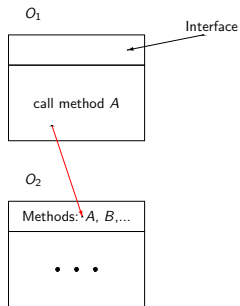
January 21, 2007

Object-Oriented



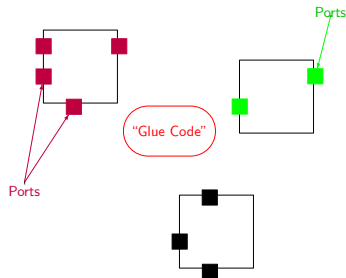
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the existence of O_2

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Component-Based



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If we want to study properties of component-based systems more information is needed.

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This means: there are three independent description levels.

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- ▶ connectors are also referred to as **maximal** interactions
- ▶ a set $Comp$ of interactions α that are called **complete**. If $\alpha \subset c$ is complete then α may proceed no matter if the missing actions of c are available or not.

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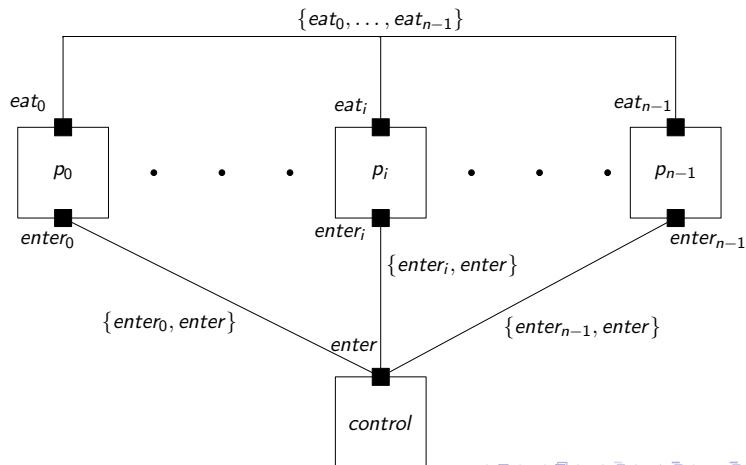
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- ▶ One component *control*. It controls when a philosopher may enter the room in which the table is located. Its ports are $\{enter, leave\}$.

Example - The Dining Philosophers, Static View

Part of the picture : the philosophers, the control and some connectors. Any nonempty subset of $\{eat_0, eat_1, \dots, eat_{n-1}\}$ is declared complete.



Dynamics of our Model

- ▶ each component i has a local behavior given by a transition system $T_i = (Q_i, \rightarrow_i)$ where $\rightarrow_i \subseteq Q_i \times A_i \times Q_i$ and A_i is the (local) port set of i . It is assumed that every state offers some action.

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- ▶ $q_i \xrightarrow{a_i} q'_i$ if $a_i \in \alpha$

Definition Interaction Systems

An **Interaction System** is given by

$$Sys = (K, C, Comp, T)$$

where

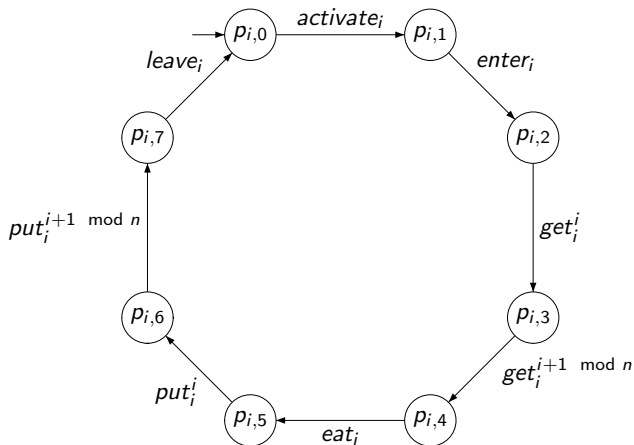
K , C , and $Comp$ constitute the static part of the system

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T constitutes the dynamic part of the system.

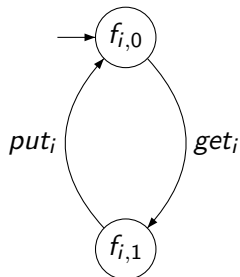
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The behavior of philosopher p_i is given by:



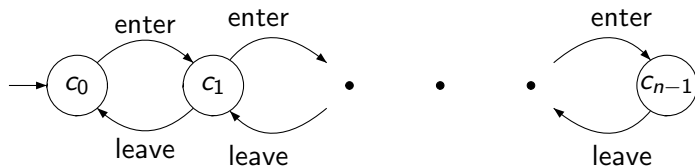
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The behavior of fork f_i is given by:



Example - The Dining Philosophers, Dynamics

The behavior of *control* is given by:



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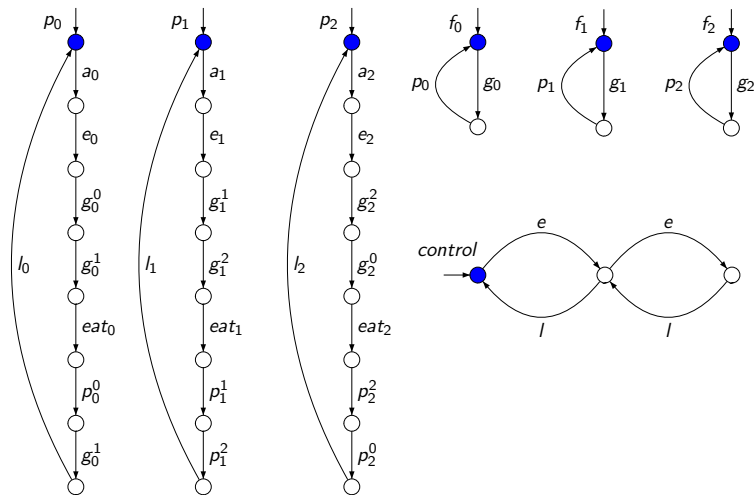
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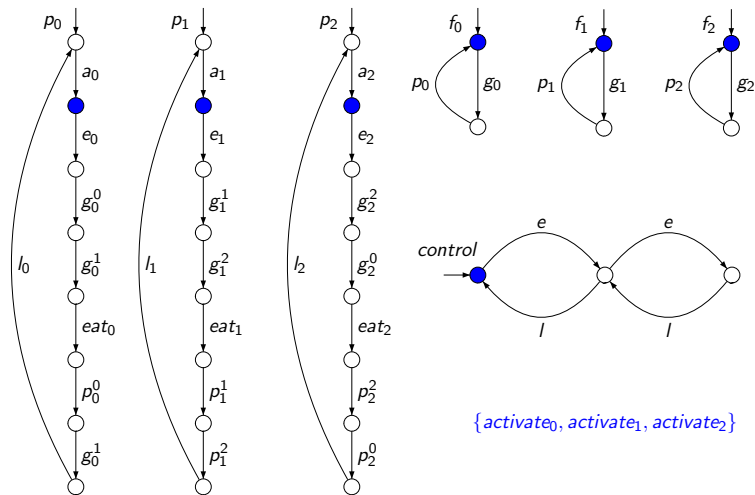
Example - The Dining Philosophers, Global Transitions

The behavior for $n = 3$:



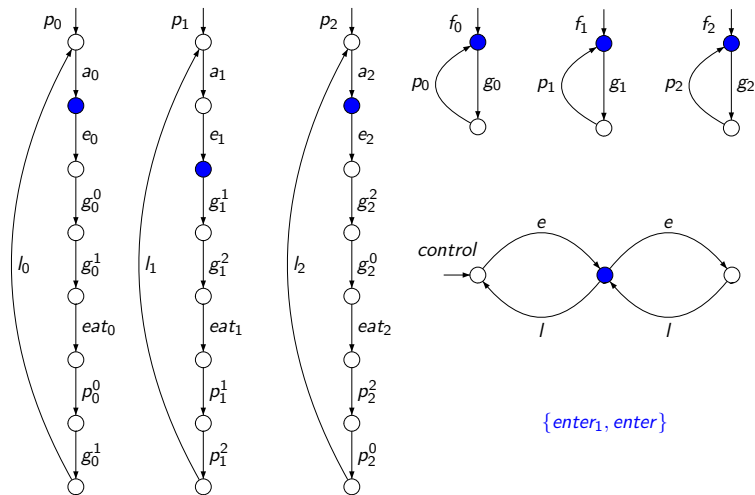
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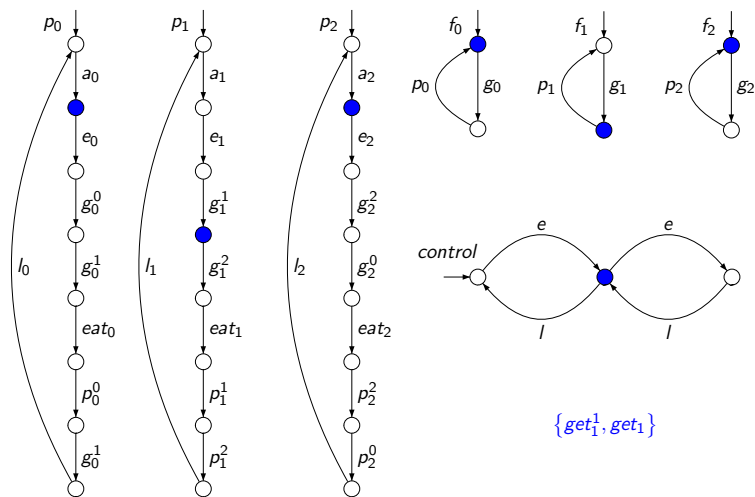
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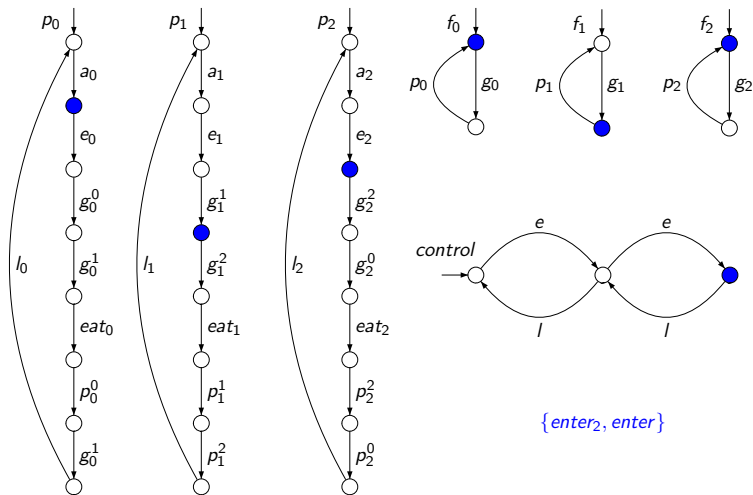
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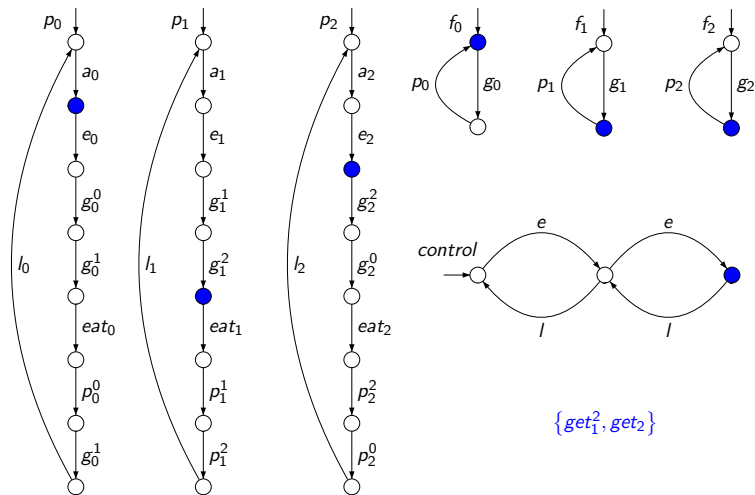
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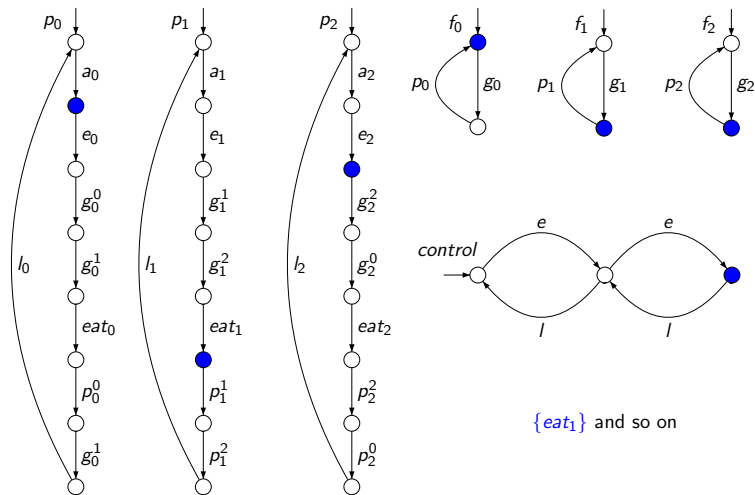
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Here we treat liveness.

A predicate P on the state space Q is **inductive** if

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Sys is called **P-deadlock-free** if for every global state q with $P(q) = \text{true}$ there is a transition

$$q \xrightarrow{\alpha} q'$$

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$K' \subseteq K$ is called **P -live** if every run with $P(q_0)$

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of Sys encompasses an infinite number of transitions labelled with an interaction where some $i \in K'$ participates.

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If $i \rightarrow j$ then j will, when it proceeds, eventually need the cooperation of i .

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But we can do better.

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$$R_{i+1}(k) = \{h \mid \forall \alpha \in C \cup \text{Comp} : h(\alpha) \neq \emptyset \Rightarrow \\ \exists j \in R_i(k) : j(\alpha) \neq \emptyset\} \cup R_i(k)$$

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$$R_0(k) = \{j \mid j \text{ reachable from } k \text{ in } G\}$$

$$R_{i+1}(k) = \{h \mid \forall \alpha \in C \cup \text{Comp} : h(\alpha) \neq \emptyset \Rightarrow \\ \exists j \in R_i(k) : j(\alpha) \neq \emptyset\} \cup R_i(k)$$

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Consider a run σ where $h \in R_1(k)$ occurs infinitely often. Then, as the system is finite, there must be some α with which h occurs infinitely often in that run. Hence there must be some component $j \in R_0(k)$ with $j(\alpha) \neq \emptyset$. Hence j participates infinitely often in σ .

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By induction on i we obtain

Theorem

Let Sys be a finite P -deadlock-free interaction system and $k \in K$ a component. If

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then k is P -live in Sys .

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Cost: graph construction and “reachability” - polynomial in $|T_i|$, $|K|$, and $|C \cup Comp|$.

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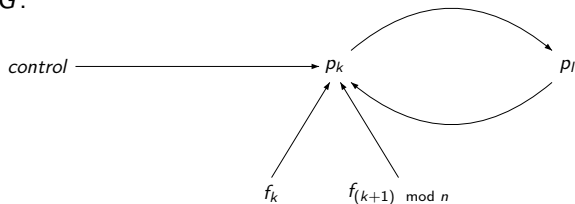
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How can it be guaranteed that no philosopher starves?

It suffices to ensure that every philosopher is live because of the linearity of the behavior of the philosophers.

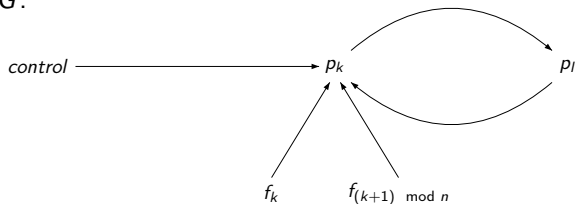
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The theorem can be used to show that every philosopher is live.
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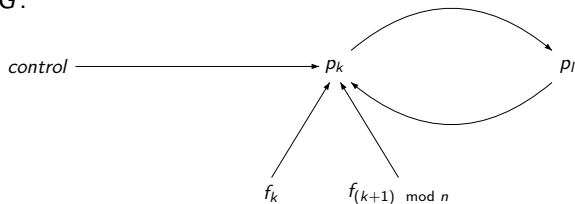
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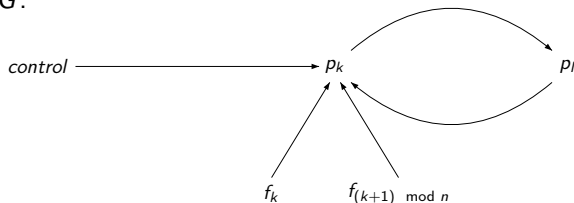
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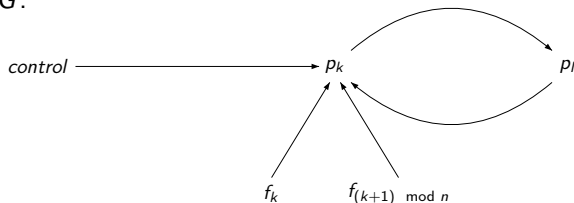
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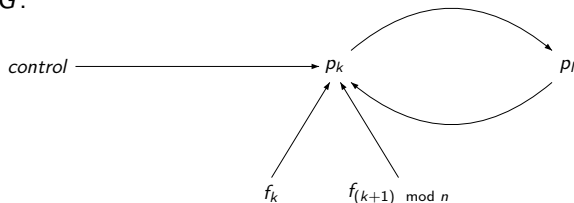
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$$\Rightarrow \bigcup_{i \geq 0} R_i(p_k) = K$$

Hence philosopher p_k is live in Sys .

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In addition we introduce probabilities to be able to make statements of the type:

With probability p no deadlock will occur.